



Comparative Analysis of Edge Detection Techniques based on MSR & PSNR

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Abstract-Edge is the boundaries of an object in image. An edge is the, rapid change in image intensity. Edge detection is applied to reduce the data and identify the edges of image and useless information is filtered out, during this process important structural features of image are preserved. In this paper, study of basic concepts of edge detection algorithms and comparative analysis of Sobel and Compass edge detection algorithms is presented with MATLAB tool. After comparing we can see that, compass edge detector performs better than sobel edge detector in terms of PSNR value, and provide sharp and less false edges. The minimum PSNR value obtained from compass edge detector is 7.0816 and that of sobel operator is 7.1236

Keywords- Edge Detection, Sobel operator, Compass Edge, MSE & PSNR

I. INTRODUCTION

Edge detection is the process of locating and identifying sharp discontinuities in image. Abrupt changes in pixel intensity are termed as discontinuities in an image. Generally in edge detection techniques, an image is convolved with an operator which is constructed so that it can be sensitive to the large gradients of image [1-2]. Various types of edge detection techniques use different operators, and depending on the applications each are sensitive to different type of edges. Selection criteria of edge operators include edge structure, edge orientation and noise environment [3-4]. For detecting the diagonal, vertical or horizontal edges operators are optimized [5]. In noisy images it is difficult to detect the edges, because edges and noise both have high frequency content. Reducing the noise from an image, results in distorted or blurred edges. In noisy images if edge operators are applied then probability of accurately localizing of detected edges becomes less [8]. Edge operator must be responsive to gradual change in the images such as poor focus and refraction. Edge detection generally has problems of high computational time, missing true edges, false edge detection, edge localization and problems due to noise. Therefore the motive is the comparative analysis of different type of edge detection techniques and performance of these in different conditions [9].

II. EDGE DETECTION TECHNIQUES

Edge detection techniques are grouped in two categories; one is gradient based edge detection, other one is laplacian based edge detection. Gradient based techniques looks for the minimum and maximum in 1st derivative of image to detect edges. Zero crossing is the criteria in 2nd derivative of image for detecting edges [13-15]. In this paper we did visual comparative analysis of compass edge detection technique and edge detection technique having sobel operator.

2.1 Sobel operator

Sobel operator has two 3×3 convolution kernels. By rotating one kernel to 90° , other kernel is obtained.

$$S_a = \begin{bmatrix} -1 & 0 & +1 \\ -2 & 0 & +2 \\ -1 & 0 & +1 \end{bmatrix}; S_b = \begin{bmatrix} +1 & +2 & +1 \\ 0 & 0 & 0 \\ -1 & -2 & -1 \end{bmatrix}$$

These masks are designed such that they respond to edges of the image running horizontally or vertically relative to pixel grid [6-7]. One kernel is for horizontal and other kernel for vertical orientation [16]. These kernels are applied on input image separately, gradient magnitude and orientation can be calculated by:

$$|S_G| = \sqrt{S_a^2 + S_b^2}; \quad (1)$$

Typically, $|S_G| = |S_a| + |S_b|$

In this operator, a RGB image is first converted into grayscale image. Then at each point magnitude of absolute gradient is calculated. Generally approximated value of gradient magnitude is calculated. That can be helpful for the faster calculations. Angle of orientation is given by:

$$\theta_g = \arctan(S_b/S_a) \quad (2)$$

2.2 Compass Edge

Compass edge uses a set of kernels which is convolved with image and these have different orientations. If N_h is the standard kernel then rotating it by 45 degree provides new kernel i.e. W_t . Similarly by rotating our standard kernel in the

range from 0 degree to 360 degree, rest of the kernels i.e. $S_h, E_t, N_h W_t, S_h W_t, S_h E_t$ and $N_h E_t$ are obtained [11-12]. In this paper we use 8 different orientations of these kernel in compass edge detection technique. In comparison to the local edge gradient the Differential gradient is time consuming [14].

$$N_h = \begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{bmatrix}; W_t = \begin{bmatrix} 0 & 1 & 2 \\ -1 & 0 & 1 \\ -2 & -1 & 0 \end{bmatrix}; S_h = \begin{bmatrix} 1 & 2 & 1 \\ 0 & 0 & 0 \\ -1 & -2 & -1 \end{bmatrix}; E_t = \begin{bmatrix} 2 & 1 & 0 \\ 1 & 0 & -1 \\ 0 & -1 & -2 \end{bmatrix};$$

$$N_h W_t = \begin{bmatrix} 1 & 0 & -1 \\ 2 & 0 & -2 \\ 1 & 0 & -1 \end{bmatrix}; S_h W_t = \begin{bmatrix} 0 & -1 & -2 \\ 1 & 0 & -1 \\ 2 & 1 & 0 \end{bmatrix}; S_h E_t = \begin{bmatrix} -1 & -2 & -1 \\ 0 & 0 & 0 \\ 1 & 2 & 1 \end{bmatrix}; N_h E_t = \begin{bmatrix} -2 & -1 & 0 \\ -1 & 0 & 1 \\ 0 & 1 & 2 \end{bmatrix}$$

magnitude is the maximum response of all kernels. Local edge gradient magnitude is given by:

$$|C| = \max (|C_i|; i = 1 \text{ to } n) \tag{3}$$

Other masks that can be used as standard kernels are Kirsch and Robinson, these are as follows:

$$K_i = \begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{bmatrix}; R_n = \begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{bmatrix}$$

2.3 MSE & PSNR

MSE stands for Mean Square Error and PSNR stands For Peak Signal to Noise Ratio. MSE is avg. pixel difference and performance of noise removal is measured using PSNR [10], MSE & PSNR calculated as:

$$MSE = \frac{1}{N} \sum_d \sum_q (S_{dq} - T_{dq})^2$$

$$(4) PSNR = 10 \log (255^2 / MSE) \tag{5}$$

N is image size, T is original image, and S is processed image

III. ANALYTICAL ANALYSIS

Sobel Operator: From section 2.1 we know that kernels used in this operator are:

$$S_a(d, q) = \begin{bmatrix} -1 & 0 & +1 \\ -2 & 0 & +2 \\ -1 & 0 & +1 \end{bmatrix}; S_b(d, q) = \begin{bmatrix} +1 & +2 & +1 \\ 0 & 0 & 0 \\ -1 & -2 & -1 \end{bmatrix}$$

For source image $A(d, q)$, first of all, source image $A(d, q)$ is to be converted into grayscale image,

$$A(d, q)_{Grayscale} = N(d, q) \tag{6}$$

Kernel $S_a(d, q)$ is convolved with the source image $A(d, q)$ which results $B(d, q)$; and then second kernel which is obtained by rotating the first kernel by 90 degree i.e. $S_b(d, q)$ is convolved with source image which results in $C(d, q)$

$$B(d, q) = S_a(d, q) * A(d, q) \tag{7}$$

$$C(d, q) = S_b(d, q) * A(d, q) \tag{8}$$

From equation (1) we know that by combining $B(d, q)$ & $C(d, q)$; at any point the absolute magnitude of Gradient can be calculated. For faster calculation, an approx. magnitude is calculated. From equation (7) and (8), Gradient Magnitude is given by:

$$D(d, q) = \sqrt{[B(d, q)]^2 + [C(d, q)]^2} \tag{9}$$

Orientation angle of edge, generally give rise to spatial gradient. The angle of orientation is given by:

$$\theta = \tan^{-1} \left[\frac{C(d, q)}{B(d, q)} \right]$$

Compass edge: First of all source image $A(d, q)$ is convolved with a standard kernel N_h giving out a function $E(d, q)$, similarly after that, this standard kernel is rotated by $45^\circ, 90^\circ, 135^\circ, 180^\circ, 225^\circ, 270^\circ, 315^\circ$ and then convolution of each of them is done with source image. Convolution of $A(d, q)$ & W_t is given by $F(d, q)$, and that of $A(d, q)$ & S_h , $A(d, q)$ & E_t , $A(d, q)$ & $N_h W_t$, $A(d, q)$ & $S_h W_t$, $A(d, q)$ & $S_h E_t$ and $A(d, q)$ & $N_h E_t$ is given by $G(d, q), H(d, q), I(d, q), J(d, q), K(d, q)$, and $L(d, q)$

$$E(d, q) = \begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{bmatrix} * A(d, q); \quad F(d, q) = \begin{bmatrix} 0 & 1 & 2 \\ -1 & 0 & 1 \\ -2 & -1 & 0 \end{bmatrix} * A(d, q);$$

$$G(d, q) = \begin{bmatrix} 1 & 2 & 1 \\ 0 & 0 & 0 \\ -1 & -2 & -1 \end{bmatrix} * A(d, q); \quad H(d, q) = \begin{bmatrix} 2 & 1 & 0 \\ 1 & 0 & -1 \\ 0 & -1 & -2 \end{bmatrix} * A(d, q);$$

$$I(d, q) = \begin{bmatrix} 1 & 0 & -1 \\ 2 & 0 & -2 \\ 1 & 0 & -1 \end{bmatrix} * A(d, q); \quad J(d, q) = \begin{bmatrix} 0 & -1 & -2 \\ 1 & 0 & -1 \\ 2 & 1 & 0 \end{bmatrix} * A(d, q);$$

$$K(d, q) = \begin{bmatrix} -1 & -2 & -1 \\ 0 & 0 & 0 \\ 1 & 2 & 1 \end{bmatrix} * A(d, q); \quad L(d, q) = \begin{bmatrix} -2 & -1 & 0 \\ -1 & 0 & 1 \\ 0 & 1 & 2 \end{bmatrix} * A(d, q);$$

Maximum response of all these kernels after convoluting with source image is calculated and it is magnitude of our absolute edge gradient. From equation (3) the absolute edge gradient magnitude can be calculated.

$$M_{max}(d, q) = \max[E(d, q), F(d, q), G(d, q), H(d, q), I(d, q), J(d, q), K(d, q), L(d, q)] \tag{10}$$

MSE & PSNR Calculations: from equation (4); (6) & (9) mean square error of images $D(d, q)$ and $N(d, q)$ is given by

$$MSE = \frac{1}{N} \sum_d \sum_q (D_{dq} - N_{dq})^2 \tag{11}$$

From equation (5) & (11)

$$PSNR1 = 10 \log (255^2 / MSE) \quad (12)$$

Similarly, from equation (4); (6) & (10) mean square error of images $M_{max}(d, q)$ & $N(d, q)$ is given by:

$$MSE = \frac{1}{N} \sum_d \sum_q (M_{dq} - N_{dq})^2 \quad (13)$$

From equation (5) & (13)

$$PSNR2 = 10 \log (255^2 / MSE) \quad (14)$$

IV. RESULT

4.1 Image A (d, q) 4.2 Image N (d, q)



Fig.1 Source Image Fig.2 Grayscale image of source image A (d, q)

4.3 Image D (d, q) 4.4 Image $M_{max}(d, q)$

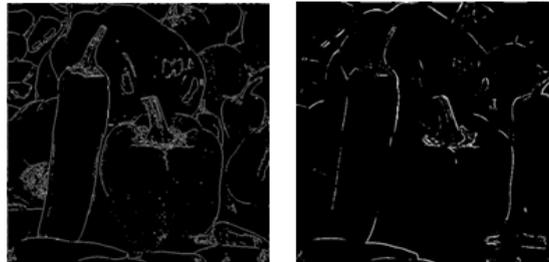


Fig.3 Output image of Sobel operator Fig.4 Output image of Compass operator

Source image A (d, q) is converted into the grayscale image i.e. N (d, q), Image D (d, q) which is sobel output image has shown more edges as compared to the image obtained after compass edge detection i.e. $M_{max}(d, q)$

Table. 1 MSE & PSNR of images with sobel and compass edge detection

Edge detection operator	MSE of Image	PSNR of Image
Sobel Operator	1.2610e+04	7.1236
Compass operator	1.2733e+04	7.0816

In table 1, MSE & PSNR of grayscale image N (d, q) and Image after applying sobel operator i.e. D (d, q) is calculated. Similarly MSE & PSNR of N (d, q) and Image after applying compass operator i.e. $M_{max}(d, q)$ is calculated.

V. CONCLUSION

Sobel operator is simple to use for detecting the edges and their corresponding orientations because it uses only two kernels, but the disadvantage of using sobel operator is that, it is very sensitive to noise and sometimes inaccurate. While on the other hand compass edge uses 8 different kernels and provides sharp edges with very less probability of detecting false edges. In terms of PSNR value compass edge performs better than sobel operator. Image D (d, q) is obtained by applying sobel operator on source image A (d, q). Grayscale image of source image A (d, q) is image N (d, q), from equation (11) & (12), MSE of D (d, q) & N (d, q) is 1.2610e+04, and corresponding PSNR value 7.1236 is calculated, similarly $M_{max}(d, q)$ is obtained by applying compass edge operator on source image A (d, q). From equation (13) (14) the MSE of $M_{max}(d, q)$ & N (d, q) is 1.2733e+04 and corresponding PSNR value is 7.0816

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