



## Hybridization between Rough Set and FLDA for Face Recognition

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**Abstract:** Face recognition is an important field of pattern recognition. Rough set theory used to extract the face from an image, by computing object lower approximation array according to gray level value. Fisher's Linear Discriminant Analysis (FLDA), was used for feature extraction and dimensionality reduction. In the proposed methods Object similarity ratio and Euclidean distance were used for classification. Experiments on ORL face database showed that the proposed methods gave promising recognition rate and acceptable test time complexity.

**Keywords:** Face Recognition, Rough Set, PCA, LDA, Euclidean Distance.

### I. INTRODUCTION

Face recognition considered as the ability to identify person based on his facial characteristics. It has been an active research area in the last decades. There are several applications to face recognition such as user authentication, security application, and criminal investigation. There exist several face recognition methods. Turk, M. and Pentland, A. [10] introduced the Eigenfaces method called Principal Component Analysis (PCA). Projecting the new image in the subspace spanned by the Eigenfaces method. PCA has become one of the most successful methods for data compression, redundancy removal, and feature extraction. Yang, J. et al [11] introduced another approach based on face representation and face recognition called Two Dimensional Principal Component Analysis (2D-PCA). 2D-PCA treats an image as a two dimensional matrix not one dimensional vector as PCA does, which reduce time used to compute eigenvectors of the covariance matrix. Both PCA and 2D-PCA do not make full use of class information. Using between class scatter matrix and within class scatter matrix LDA [12] tried to find a set of projection vector to solve this problem. A very powerful tool used in the field of image analysis is called wavelet transform. The multiresolution decomposition provides a useful image representation for vision algorithms [5]. A lot of researchers integrated the DWT with other algorithms to improve recognition rate. Song, L. and Min, L. [9] integrate DWT with 2D-PCA algorithm for feature extraction and got recognition rate 92% on ORL database. Mohie El-din, M.M. et al, [3, 2] proposed a hybrid method of DWT, 2D-PCA and LDA that enhanced recognition rate to 97.5% using ORL database. In addition Rough Set Theory was used in [7] for image retrieval. B. Debotosh et al, [1] integrated rough set to reduce the feature vector generated by the PCA algorithm. Authors in [4] presented a hybrid system consisting of PCA, Rough Set and Neural Network for dimensionality reduction and classification in human face recognition. This method was tested on a well known ORL face database and gave 93% average recognition rate.

In this paper three methods are introduced for face recognition problem. This methods integrated Rough Set with FLDA, Object Similarity Ratio and Euclidean Distance, which gave high recognition rate and minimize time consumed in testing stage. The rest of this paper is organized as follows: Section 2 describes existing techniques PCA, LDA, Rough Set, Euclidean distance and Object similarity ratio. Section 3 describes the proposed methods. The proposed methods are evaluated in Section 4 by performing tests on a well known ORL face database. Section 5 contains conclusion and future work.

### II. FACE RECOGNITION METHODS

This section describes some of existing techniques for face recognition problem.

#### 2.1 Rough Set preliminaries

Rough set theory depends on the idea that every object is associated with a piece of knowledge indicating relative membership. Knowledge is represented by means of a table, so-called an information system, where rows and columns respectively denote objects and attributes. Consider an information system,  $S$ , is given as a pair  $S=(U,A)$  where  $U$  is a non-empty finite set of objects, as the universe, and  $A$  is a non-empty finite set of attributes. Let  $B \subseteq A$  and  $X \subseteq U$ . We can approximate the set  $X$  using only the information contained in  $B$  by constructing the lower and upper approximations of  $X$ . If  $X \subseteq U$ , the sets  $\{x \in U : [x]_B \subseteq X\}$  and  $\{x \in U : [x]_B \cap X \neq \Phi\}$ , where  $[x]_B$  denotes the granule in other words equivalence class of the object  $x \in U$  relative to the equivalence relation  $I_B$ , are called the  $B$ -lower and  $B$ -upper approximations of  $X$  in  $U$ . They are denoted by  $BX$  and  $\overline{BX}$ , respectively. Figure 1 show the representation of a set  $X$  with the upper and lower approximation. Set of dark gray granules represent lower approximation, set of dark gray and light gray granules represent upper approximation.

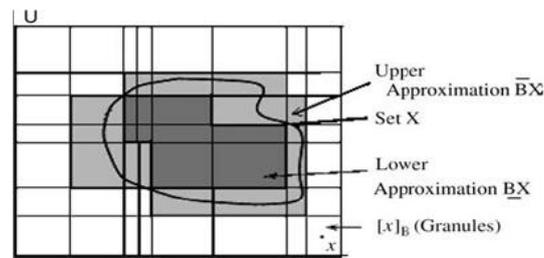


Figure 1: Rough Representation of a Set X

Assume the universe U be an image consisting of a collection of pixels, partition U into a collection of non overlapping windows, each window can be considered as a granule G. Granulation involves decomposition of whole into parts [8]. Let us consider an object-background separation (a two class) problem of an mn gray scaled image with gray level intervals (0,1, T,T+1, ...,L-1) with L gray levels; Let B and O represent two properties that characterize background and object regions, respectively Object and background can be viewed as two sets with their rough representation with respect to gray level T. Lower approximations of the object  $O_T$  :

$$\underline{O}_T = \{ \bigcup_i G_i | P_j > T, \forall j = 1, \dots, mn, \text{ and } P_j \text{ is a pixel belonging to } G_i \}.$$

Upper approximation of the object  $\bar{O}_T$ :

$$\bar{O}_T = \{ \bigcup_i G_i, \exists j, j = 1, \dots, mn, \text{ s.t. } P_j > T, \text{ where } P_j \text{ is a pixel in } G_i \}.$$

Lower approximations of the background  $\underline{B}_T$  :

$$\underline{B}_T = \{ \bigcup_i G_i | P_j \leq T, \forall j = 1, \dots, mn, \text{ and } P_j \text{ is a pixel belonging to } G_i \}.$$

Upper approximations of the background  $\bar{B}_T$ :

$$\bar{B}_T = \{ \bigcup_i G_i, \exists j, j = 1, \dots, mn, \text{ s.t. } P_j \leq T, \text{ where } P_j \text{ is a pixel in } G_i \}.$$

Thus the roughness of the object at gray level value T is given by:

$$R_{O_T} = 1 - \frac{|\underline{O}_T|}{|\bar{O}_T|} = \frac{|\bar{O}_T| - |\underline{O}_T|}{|\bar{O}_T|} \quad (1)$$

Also, the roughness of the background at gray level value T is given by:

$$R_{B_T} = 1 - \frac{|\underline{B}_T|}{|\bar{B}_T|} = \frac{|\bar{B}_T| - |\underline{B}_T|}{|\bar{B}_T|} \quad (2)$$

Where  $|\underline{O}_T|$ ,  $|\bar{O}_T|$ ,  $|\underline{B}_T|$  and  $|\bar{B}_T|$  denotes the cardinality of the lower and upper approximations for object and background respectively.

The mean roughness at a certain threshold T is defined as

$$RM_T = \frac{R_{O_T} + R_{B_T}}{2} \quad (3)$$

We select T which minimize the mean roughness[8]. Figure 2 show a flow chart of how to select the optimal threshold T.

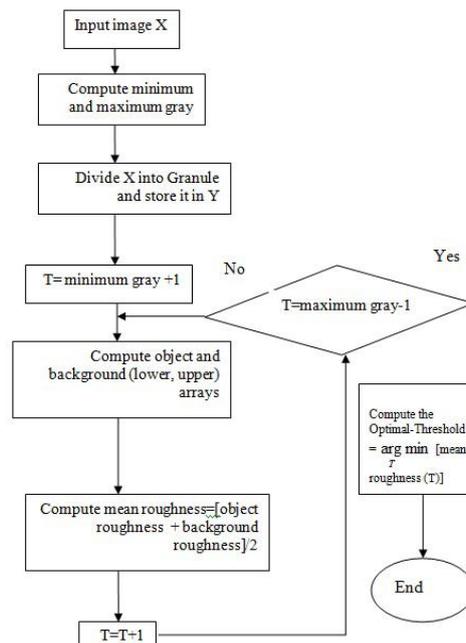


Figure 2: Flow chart of T selection

## 2.2 Principal Component Analysis

The principal component analysis (PCA) is a statistical model used for face recognition, one of the most successful techniques that have been used in image processing. The purpose of PCA is to reduce dimensionality of the data space to the smaller intrinsic dimensionality of the feature space [?], which are needed to describe the data economically. This reduction is realized by the linear transformation.

$$Y = AX. \quad (4)$$

Where Y is the feature matrix, A is the transformation matrix and X is the original image. PCA can give us data compression, prediction, redundancy removal, feature extraction. The scope of using PCA for face recognition is to express the large one dimensional vector of pixel constructed from the two dimensional facial image into the compact principal components of the feature space. This is called eigenspace projection. Eigenspace can be calculated by calculating the eigenvectors of the covariance matrix derived from dataset of images. In 1991, Eigenfaces method was firstly introduced by M. Turk and A. Pentland [10]. Assume we have a set of N images  $X_1; X_2, \dots, X_N$ . Originally, each image is a 2-dimensional matrix of size m by n. PCA converts each image to 1-dimensional column vector of size m as follows.

$$X_i = \begin{pmatrix} x_1 \\ x_2 \\ \vdots \\ x_{mn} \end{pmatrix} \quad (5)$$

The images set is

$$X = [X_1, X_2, \dots, X_N] \quad (6)$$

then compute the mean image  $X_m$  as follows

$$X_m = \frac{1}{N} \sum_{i=1}^N X_i. \quad (7)$$

and the covariance matrix is given by the formula

$$C = \frac{1}{N} \sum_{i=1}^N (X_i - X_m)(X_i - X_m)^T. \quad (8)$$

Let  $W_i = (X_i - X_m)$ , be the centered image. Now we want to find the eigenvalues  $\lambda_i$  and eigenvectors  $e_i$  of the covariance matrix C.

$$C = WW^T. \quad (9)$$

Where W is a matrix composed of the column vector  $W_i$  placed side by side. The size of C is  $mn \times mn$ , so image of size  $100 \times 100$  will create a covariance matrix of size  $10000 \times 10000$  which will not be practical to solve for the eigenvectors of C directly. A theorem in linear algebra states that the vectors  $e_i$  and scalars  $\lambda_i$  can be computed by solving for the eigenvectors and eigenvalues of the  $N \times N$  matrix  $WTW$  [10]. Let  $d_i$ ,  $\mu_i$  be the eigenvectors and eigenvalues of  $WTW$ , respectively.

That is mean that

$$W^T W d_i = \mu_i d_i \quad (10)$$

By multiplying both sides by W (from left)

$$(WW^T) W d_i = \mu_i (W d_i) \quad (11)$$

Which mean that the first  $N \times 1$  eigenvectors  $e_i$  and eigenvalues  $\lambda_i$  of the covariance matrix  $C = WW^T$  are given by  $W d_i$  and  $\lambda_i$ , respectively.  $W d_i$  needs to be normalized in order to be equal to  $e_i$ . Since we have a finite number of image vectors, N and the rank of the covariance matrix can not exceed  $N \times 1$  (because we subtract the mean vector m). PCA transformation matrix A can be constructed from the eigenvectors corresponding to the k largest eigenvalues of the covariance matrix C.

## 2.3 Fisher's Linear Discriminant Analysis

PCA do not make full use of class information. Using **between class scatter matrix** ( $S_B$ ) and **within class scatter matrix** ( $S_W$ ), Fisher's Linear Discriminant Analysis, (FLDA), [12] tried to find a set of projection vector to solve this problem. FLDA is a good example for class specific method, since the training set is labeled, it make sense to use this class information to build a more reliable method to reduce the dimension of the feature space. FLDA maximizes the ratio of the  $S_B$  matrix and  $S_W$  matrix and Looks for a linear subspace  $W$  (c-1 component) in which the projection of the different classes are best separated. Let  $Y = \{y_1, y_2, \dots, y_N\}$  be a set of N samples in d dimensional space. Let  $l_i$  be class label of  $Y_i$ ,  $l_i \in \{1, 2, \dots, c\}$ , c is classes number, denote class i sample number by  $N_i$ . Then the between class scatter matrix is defined as

$$S_B = \sum_{i=1}^C N_i (\mu_i - \mu)(\mu_i - \mu)^T \quad (12)$$

Within class scatter matrix is defined as

$$S_W = \sum_{i=1}^C \sum_{k=1}^{N_i} (Y_k - \mu_i)(Y_k - \mu_i)^T \quad (13)$$

Where the mean of the  $i_{th}$  class is

$$\mu_i = \frac{1}{N_i} \sum_{j=1}^{N_i} Y_j \quad (14)$$

Total class scatter matrix is

$$S_T = \sum_{i=1}^N (Y_i - \mu)(Y_i - \mu)^T \quad (15)$$

where  $\mu$  is the global mean of all samples.

$$\mu = \frac{1}{N} \sum_{k=1}^N Y_k \quad (16)$$

FLDA look for  $W_{opt}$  which is the optimal projection matrix for maximizing the discriminant criteria

$$W_{opt} = \frac{|W^T S_B W|}{|W^T S_W W|} \quad (17)$$

If  $S_W$  is nonsingular, then  $W_{opt}$  is the matrix with the orthonormal columns which maximizes ratio of the determinant of the  $S_B$  matrix to the determinant of the  $S_W$  matrix of the projected sample,

$$W_{opt} = \arg \max_W \frac{|W^T S_B W|}{|W^T S_W W|} \quad (18)$$

$$W_{opt} = (W_1, W_2, W_3, \dots, W_m) \quad (19)$$

such that  $W_i, i = 1; 2 \dots m$  is the set of the generalized eigenvectors of the  $S_B$  and  $S_W$  matrices corresponding to the  $m$  largest eigenvalues  $\lambda_i; i = (1; 2 \dots m)$ .

$$S_B W_i = \lambda_i S_W W_i, i = (1, 2, 3 \dots m) \quad (20)$$

The upper bound of  $m$  is  $c-1$  where  $c$  is the number of classes in the training sample. If  $S_W$  is singular, PCA is implemented to reduce dimensionality of the training images to solve this problem, and then FLDA is implemented to reduce dimensionality to  $c-1$ . Assume that

$$W_{Pca} = \arg \max_W |W^T S_T W| \quad (21)$$

be the PCA transformation matrix,

$$W_{flda} = \arg \max_W \frac{|W^T W_{Pca}^T S_B W_{Pca} W|}{|W^T W_{Pca}^T S_W W_{Pca} W|} \quad (22)$$

be the FLDA transform matrix, then the optimal projection matrix  $W_{opt}$  is given by

$$W_{opt} = W_{Pca} W_{flda} \quad (23)$$

## 2.4 Euclidean Distance

Euclidean distance is used as the classifier to identify the image in the training set to which the test image belong. Image classification is performed by comparing the feature vectors (weight matrix) of the images in the training set with the feature vector (weight matrix) of the test image using Euclidean distance,

$$\varepsilon_i = \|\Omega_T - \Omega_i\| \quad (24)$$

where  $i$  is a vector describing the  $i_{th}$  face image in the training set.

## 2.5 Object Similarity Ratio

In order to match between two objects in different images, we compute the object lower approximation array for each images. Then the object similarity ratio[7] is computed as follows:

$$ObjectSimilarityRatio = \frac{N}{T} \quad (25)$$

Where  $N$  denotes the number of pixels, which are the same in two object lower approximation arrays (Test image, Training image) and  $T$  is the size of the object lower approximation array. object similarity ratio equal 1 if the two images are the same, otherwise between  $[0; 1]$ . The recognition system retrieve image which have the large object similarity ratio.

### III. PROPOSED METHOD

In the proposed methods, we compute the object lower approximation array for all images in the database. Images is divided to two sets (training and testing). FLDA is used to extract the feature from the object lower approximation arrays for training images. Minimum Euclidean Distance is used to compute the distance between the test image and images in the training set. Figure 3, Figure 4 and Figure 5 show a block diagram of the proposed methods.

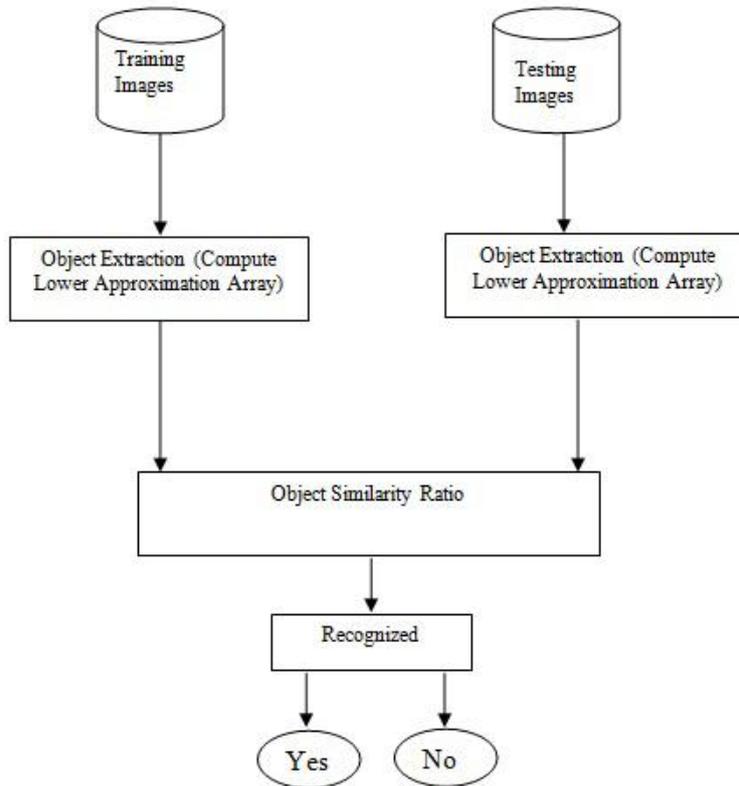


Figure 3: Rough Set and Object Similarity Ratio Method

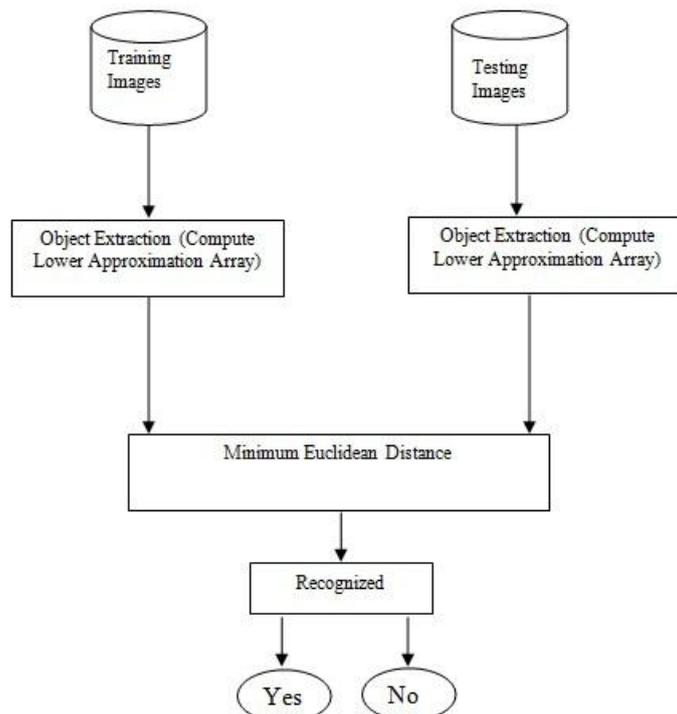


Figure 4: Rough Set and Euclidean Distance Method

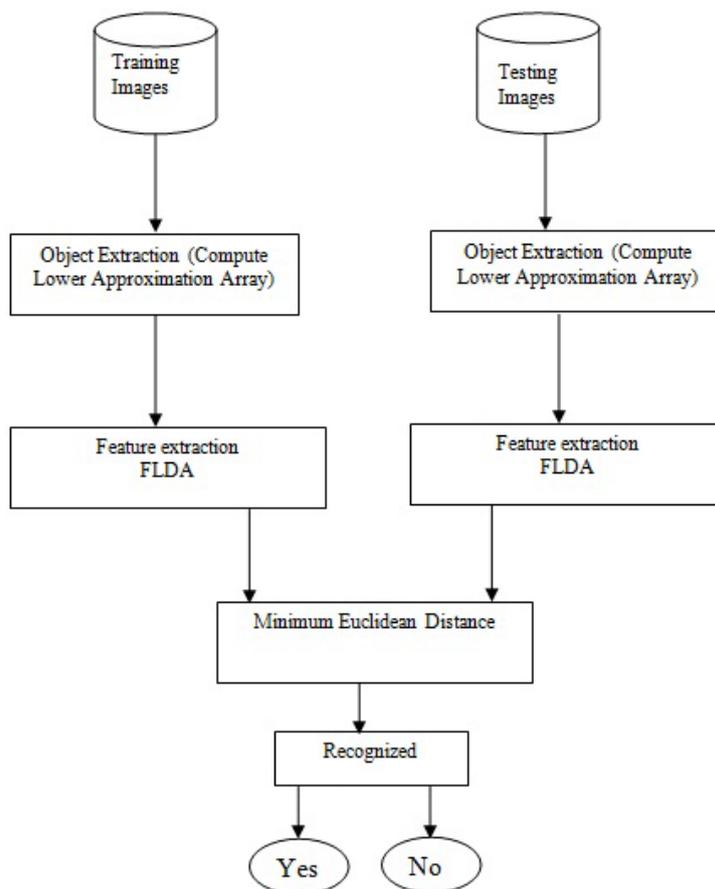


Figure 5: Rough Set and FLDA Method

#### IV. EXPERIMENTAL RESULTS

##### 4.1 Face Database

Experiments were carried out on a well known ORL face database [6]. Sample of the ORL images is shown in Figure 6. This database contains 40 classes; each class contains 10 images for each person. The images are taken in different periods, different facial expression and facial details such as smiling, eye open, eye closed, wearing glasses or not, different illumination, total of 400 images. In the experiment some images are used to establish training set and the rest is left for the testing stage.



Figure 6: Sample of ORL Face Database

##### 4.2 Results

In order to compute the object lower approximation array for all images in the given ORL face database(400 images), it takes 414 seconds. Then object similarity ratio and Euclidean distance were used to classify the test images. To reduce time, FLDA was used for dimensionality reduction. Table 1 show the recognition rate of the proposed methods. When Rough set integrated with FLDA, recognition rate between 90%, 97.5%, but when we use Rough set Object similarity ratio method recognition rate was between 90.5% and 100%. Table 2 show a comparison of testing time complexity for the different methods. It is clear that integrating FLDA and rough set gave significant improvement in time complexity.

Table 1: Comparison of Recognition Rates on ORL Database

no of training images	Rough Set - Object Similarity Ratio	Rough Set - Euclidean Distance	Rough Set - FLDA	PCA_Rough set_Neural network [4]
5	90.5	91	90	...
6	98	94.37	94.37	...
7	99.17	95.8	95	...
8	100	95	96.25	...
9	100	92.5	97.5	...
average	97.5	93.73	94.6	93

Table 2: Comparison of Testing Time Complexity(Seconds) on ORL Database

no of training images	Rough Set - Object Similarity Ratio	Rough Set - Euclidean Distance	Rough Set - FLDA
5	8.35	4.83	2.57
6	7.64	4.52	2.35
7	6.61	3.8	2
8	5	2.86	1.5
9	2.91	1.6	1.22

## V. CONCLUSION

In this paper different methods were examined. Results show that when Rough set Object similarity ratio method was used, it gave high recognition rate between 90.5% and 100%. Note that time complexity was very high in this method compared with the other methods between 2.91 and 8.35 seconds. When Euclidean distance was used with Rough set, recognition rate was between 91% and 95.8%, but in this method test time complexity was diminished with 41%. Rough set FLDA gave recognition rate between 90% and 97.5%. Also, test time complexity was diminished with 66% compared with Rough set Object similarity ratio method. Future Work in connection to this paper will test these methods using different databases, try to enhance recognition rate in case of small training sample size and try to decrease time consumed in object lower approximation array computation.

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