



Robust Watermarking Of Greyscale Images In Frequency Domain Using M Sequences Correlation Properties

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Abstract— Proliferation of internet, together with relatively inexpensive digital recording and storage peripherals has created an era where duplication, unauthorized use and maldistribution of digital content has become easier. Thus, protection of Intellectual Property Rights (IPS) is of great importance to prevent unauthorized use, misappropriation and misrepresentation. Digital watermarks are pieces of information added to digital data (audio, video, or still images) that can be detected or extracted later to make an assertion about the data, thereby providing protection for IPS. This information can be textual data about the author, its copyright, etc. or it can be an image itself. This watermark in a document assert the ownership of the document. In case of image watermarking, it is often the requirement that watermark should be invisible to human. Also, unauthorized removal and detection of the watermark must be impossible even if the watermarking scheme is partially known. A digital watermark in an image can be embedded in spacial (pixels values) or in transform (Discrete Fourier, Discrete Cosine, etc.) domain. In this work, a technique for watermarking of grayscale images in frequency domain is presented. A phase-based signature of the image, modulated by PN (Pseudo Noise) sequence, is hid into its Fourier magnitude spectrum in the embedding stage. The detector computes the Fourier transform of the watermarked image and extracts the embedded signature. The proposed method provides blind detection at the receiver which is a major advantage, due to the fact that neither original data knowledge nor time consuming search in owners' database is needed for watermark detection and extraction. Experimental results indicate the ability of the proposed method to deal with the a large class of attacks. Results are compared with existing techniques and conclusions are provided.

Keywords— Watermarking, Greyscale Images, Fourier Transform, PN sequences, M sequences, Spread Spectrum

I. BPOF as watermark

Binary phase-only filter (BPOF), is an inherent characteristic of an image, and this can serve as the basis for watermark [23] One can start with the spatial realization of an image, which is the luminance values of the pixels (bitmap). Then the 2-dimensional Discrete Fourier transform (DFT) to the bitmap or a single 1 D DFT to the complete pixel array taken row wise can be applied . The watermarking process hides into the image, the BPOF, thus forming the watermarked image. This hiding is done by changing, in a specific manner, the magnitude of the Fourier coefficients, based on the BPOF. This change is done in a judicious manner so that the image is not visually degraded, while at the same time, the changes are such that these cannot be lost due to noise or compression. Then the inverse transform is applied to the image, thereby getting back the watermarked image. This technique can be attacked so that the watermark can be removed and hence a false negative can be achieved, but in the proposed work, the matching of the extracted information to the BPOF is accomplished using correlation metrics thereby providing robust watermarking.

II. Modulated BPOF with m sequence as a watermark

The process of embedding the watermark in frequency domain is accomplished by first converting the image pixel values to Fast Fourier Transform. FFT is a reversible transformation which provides perfect reconstruction of the original values. As per the requirement of the FFT algorithm to process the data samples of size in the power of two, it is the requirement of the algorithm that the number of pixels in the host image must be a power of two. This includes images of dimension 64X64, 128*128, 128X64 and likewise. Nevertheless, the scheme presented in the current work can be applied to watermark image of any dimension. The Binary Phase only Filter (BPOF) of the original Image is obtained using the phase values from the Fast Fourier Transform of the original image. This BPOF is then modulated by PN sequence which is used as the digital watermark of the original image. The process of embedding watermark using FFT in grayscale images is described in the following algorithm.

Algorithm: Embedding

1. Let the given image has n pixels, where $n = 2^k$ for some $k \in \mathbb{I}^+$. Tabulate the pixel values of grayscale image row-wise starting from the top left corner. These values belongs to the range from 0 to 255, giving a total of 256 colors giving shades of grey from 0 as black to 255 as white covering all shades of grey in between these limits.
2. Obtain the FFT of the data values. These values are complex numbers of the form $a+ib$, where i is $\sqrt{-1}$. Convert these values in the form $Ae^{i\theta}$, where A is the magnitude and $e^{i\theta} = \cos\theta + i \sin\theta$.

3. Calculate the Binary Phase Only Filter (BPOF) as per the following scheme. For any sample value n, if $\cos\theta > 1$, BPOF (n) = 1, else 0.
 4. Modulate the BPOF using PN sequence obtained through LFSR. This BPOF is a bipolar binary image of the original image, which has been shown to possess a number of discriminatory features of the original image.
 5. Using the Logical Reversible Operation XOR, operate the modulated BPOF with m^{th} bit plane and replace k^{th} bit plane with the resultant.
 6. Obtain the Inverse DFT of the sample values and get the pixel values of the watermarked image.
- This scheme is illustrated with the following example. Consider the pixel value matrix of any image as shown in figure 1.

251	200	255	244	199	201	160	177
121	199	201	160	177	201	160	200
188	150	200	199	177	201	160	200
199	144	159	177	201	160	177	177
177	201	160	200	232	199	180	200
200	200	130	199	177	201	160	200
199	270	177	201	160	200	188	129
121	177	201	160	200	199	198	133

Figure 1 An arbitrary portion of grayscale image of 8X8 pixels

Given a sequence of N samples $f(n)$, indexed by $n = 0..N-1$, the Discrete Fourier Transform is defined as $F(k)$, where $k=0..N-1$:

$$F(k) = [1/\sqrt{N}] * \sum_{n=0}^{N-1} f(n) e^{-i2\pi kn/N}$$

$F(k)$ are often called the 'Fourier Coefficients' or 'Harmonics'.

The sequence $f(n)$ can be calculated from $F(k)$ using the Inverse Discrete Fourier Transform (IDFT)

$$f(n) = [1/\sqrt{N}] * \sum_{k=0}^{N-1} F(k) e^{i2\pi kn/N}$$

The factor $[1/\sqrt{N}]$ is sometimes skipped for the sake of fast computations. The frequency domain representation, using DFT, of the pixel values, taken row wise, starting from top left corner, is shown in the figure 2.

11904	84.59897 35532825 +91.5860 90078916 4i	109.95 42537 78935 - 196.77 06879 87655i	265.8829 81467977 - 82.48398 46089861 i	388.70 46939 77262 - 290.27 76824 83071i	249.937523 415086+11 6.40777159 5575i	- 94.114 07674 32181 - 54.792 88521 22747i	- 103.549 604053 545- 289.195 840039 834i
- 169.530 4832720 5- 172.831 9984622 14i	- 62.78187 73779053 - 157.5984 04017927 i	- 165.85 92516 29507 - 91.631 87518 99344i	- 38.81943 17278381 - 93.92108 38634986 i	38.035 23851 89684 - 71.139 86680 04932i	154.604760 862055+12 4.05360926 8126i	35.224 24954 04475 +90.5 39686 81120 47i	- 437.318 558780 238- 218.105 033079 495i
113- 147i	- 77.70361 474352- 125.0058 15630618 i	58.265 56554 77258 - 59.306 67272 65793i	205.1384 78050536 +114.744 53485600 5i	157.22 96967 44737 +35.7 96208 06257 74i	317.343506 999774+38 .879228650 2638i	16.078 96128 04672 - 159.19 32427 31837i	- 165.977 577592 822+99. 130556 637819 9i
35.5304 8327204 93+27.1	335.9160 90261481 +28.2018	9.0861 42503 04412	200.8225 98489014 +63.7574	112.03 03707 59032	125.215699 613699- 194.900539	359.36 41557 22103	130.690 051562 962+15

6800153 77854i	76608693 7i	+6.58 18221 08893 23i	57671813 3i	- 131.34 16076 2i	708124i	- 209.68 09726 62368i	1.69720 927108 5i
-214	130.6900 51562962 - 151.6972 09271085 i	359.36 41557 22104 +209. 68097 26623 67i	125.2156 996137+1 94.90053 9708124i	112.03 03707 59032 +131. 34160 762i	200.822598 489014- 63.7574576 718135i	9.0861 42503 0445- 6.5818 22108 89345i	335.916 090261 481- 28.2018 766086 949i
35.5304 8327204 94- 27.1680 0153778 57i	- 165.9775 77592822 - 99.13055 66378193 i	16.078 96128 04679 +159. 19324 27318 37i	317.3435 06999775 - 38.87922 86502647 i	157.22 96967 44737 - 35.796 20806 25776i	205.138478 050536- 114.744534 856006i	58.265 56554 77261 +59.3 06672 72657 92i	- 77.7036 147435 187+12 5.00581 563061 8i
113+147 i	- 437.3185 58780237 +218.105 03307949 7i	35.224 24954 04475 - 90.539 68681 12044i	154.6047 60862054 - 124.0536 09268126 i	38.035 23851 89683 +71.1 39866 80049 35i	- 38.8194317 278379+93 .921083863 499i	- 165.85 92516 29506 +91.6 31875 18993 5i	- 62.7818 773779 047+15 7.59840 401792 7i
- 169.530 4832720 49+172. 8319984 62215i	- 103.5496 04053544 +289.195 84003983 5i	- 94.114 07674 3218+ 54.792 88521 22752i	249.9375 23415086 - 116.4077 71595575 i	388.70 46939 77262 +290. 27768 24830 71i	265.882981 467977+82 .483984608 9856i	109.95 42537 78936 +196. 77068 79876 55i	84.5989 735532 823- 91.5860 900789 163i

Figure 2 FFT sample values of the pixel values of fig 3.1

It is clear from the table that the first entry is the sum of all the values of individual pixels, the second entry is the complex conjugate of the last entry and likewise.

III. Computing (BPOF) from FFT

The Binary Phase only Filter (BPOF) signature can be obtained by converting the complex sample values to the form $Ae^{i\theta}$ and computing the phase of the sample values. It is worth mentioning here that

$$e^{i\theta} = \cos\theta + i \sin\theta.$$

BPOF sample value is 0 if $\cos\theta < 1$, and 1 otherwise. BPOF possess several properties of the original image and can itself be used as a watermark or a digital signature. The BPOF signature for the above sample values can be obtained as shown in figure 3.

1	1	1	1	1	1	0	0
0	0	0	0	1	1	1	0
1	0	1	1	1	1	1	0
1	1	1	1	1	1	1	1
0	1	1	1	1	1	1	1
1	0	1	1	1	1	1	0
1	0	1	1	1	0	0	0
0	0	0	1	1	1	1	1

Figure 3 BPOF signature corresponding to FFT sample values fig 3.2

It is clear from the above table that like the Discrete Fourier Transform of the original image pixel values, the BPOF also follows the same pattern that except, the starting value of the BPOF, the rest of the values follows after half of the sample values in reverse order. Thus, for a total of 64 sample values, BPOF of first 33 values can give the BPOF of the entire

pixel values. This result is straightforward as out of the total 2^n sample values of the DFT, two values are real numbers and the rest of the sample values can be partitioned into two parts with each value being complex conjugate of the other. This similar result hold for BPOF which can be obtained by diving the real part of the complex number with the absolute value of the complex number. Thus, the first $2^{n-1}+1$ values of BPOF can give the entire sequence of the BPOF. For a table consisting of 2^n values, the BPOF (and also the DFT) values form the pattern as shown in Table 1.

TABLE 1 CONJUGATE PROPERTY OF FFT AND CORRESPONDING EFFECT ON BPOF

Sample Data Values	DFT	Analysis
Value 1 (v1)	Sum(v1,v2..vn)	Only these first $2^{n/2}+1$ values of DFT are sufficient to generate the entire sequence. Same is the case with BPOF.
Value 2 (v2)	Complex Number 1 (c1)	
Value 3 (v3)	Complex Number 2 (c2)	
.		
.		
.		
Value $2^{n-1} + 1.(v2^{n-1} + 1)$	Real Number $2^{n-1} + 1 (c 2^{n/2} + 1)$ (obtained by summing all the sample values, with negatives of alternate values starting from the second value.)	
.		
.		
.		
Value $2^n - 1(v2^n - 1)$	Complement of Complex Number 2 (c2)	
Value $2^n (v2^n)$	Complement of Complex Number 1 (c1)	

Thus, for a total of 2^n values of BPOF, the first $2^{n-1}+1$ values can generate the entire sequence as they are repeated again in the subsequent values in reverse order.

Consider only the first $2^{n-1} + 1$ values of the BPOF. Further, considering only the values except first and the last, these are total $2^{n-1}-1$ values, which is equal to the length of code generated by an LFSR circuit having n-1 registers.

IV. Watermark Embedding

In the current scheme of 8X8 block size, watermarking procedure is operated on DFT samples from 2^{nd} to 32^{nd} sample, as it can be inverted to obtain the second half of DFT values.

The magnitude of the corresponding complex numbers can be tabulated as shown in figure 4.

101110	000000	00000	00000	000	00000	000	00000
100000	011111	01110	10001	001	10001	000	10011
00	01	0001	0110	111	0100	011	0011
				001		011	
				01		01	
000000	000000	00000	00000	000	00000	000	00000
111100	101010	01011	00110	000	01100	000	11110
10	10	1101	0110	010	0110	011	1001
				100		000	
				01		01	
000000	000000	00000	00000	000	00000	000	00000
101110	100100	00101	01110	000	10100	000	01100
01	11	0011	1011	101	0000	101	0001
				000		000	
				01		00	
000000	000001	00000	00000	000	00000	000	00000
001011	010100	00000	01101	000	01110	001	01100
01	01	1011	0011	101	1000	101	1000
				011		000	
				01		00	
000000	000000	00000	00000	000	00000	000	00000
110101	110010	11010	01110	000	01101	000	10101
10	00	0000	1000	101	0011	000	0001
				011		010	
				01		11	
000000	000000	00000	00000	000	00000	000	00000
001011	110000	01010	10100	000	01110	000	01001
01	01	0000	0000	101	1011	010	0011
				000		100	

				01		11	
000000	000001	00000	00000	000	00000	000	00000
101110	111010	00110	01100	000	00110	000	01010
01	01	0001	0110	010	0110	101	1010
				100		111	
				01		01	
000000	000001	00000	00000	000	00000	000	00000
111100	001100	00110	10001	001	10001	000	00111
10	11	1101	0100	111	0110	111	1101
				001		000	
				01		01	

Figure 4 Magnitude of the complex sample values of figure 3.3

Consider the m sequence of length 31, 1010111011000111110011010010000.

The 31 consecutive values of the BPOF, starting from the beginning and except the first value are as follows:

111110000001110101111011111111

The Bitwise Exclusive OR operation on m sequence with the 31 bits (excluding first) of BPOF, yields the sequence as shown in figure 3.5.

The XOR operation is a reversible operation which can produce any of the inputs by again operating the output with any other input.

This Output is then substituted by the nth bit of the input, depending upon the required robustness

Replacing the 4th bit plane with the XOR output for all 64 values of DFT, one can have the following values as shown in figure 6.

10111	0000	0000	00000	0000	0000	0000	00000
01000	0001	0011	10001	0111	0100	0001	10011
0000	1101	1010	0110	1011	0101	1011	1011
(Intact)	01	01		01	00	01	
00000	0000	0000	00000	0000	0000	0000	00000
01111	0010	0010	00110	0001	0011	0001	11110
0010	1010	1111	0110	0110	0011	1000	1001
	10	01		01	10	01	
00000	0000	0000	00000	0000	0000	0000	00000
01011	0010	0001	01110	0010	0101	0010	01100
0001	0110	0100	1011	1010	0000	1000	0001
	11	11		01	00	00	
00000	0000	0000	00000	0000	0000	0000	00000
00010	0101	0000	01101	0010	0011	0110	01100
0101	0110	0010	0011	1011	1010	1010	1000
	01	11		01	00	00	
00000	0000	0000	00000	0000	0000	0000	00000
01101	0011	0110	01110	0010	0011	0000	10101
0110	0010	1010	1000	1011	0100	0010	1001
(Intact)	00	00		01	11	11	
00000	0000	0000	00000	0000	0000	0000	00000
00010	0011	0010	10100	0010	0011	0001	01001
0101	0000	1000	0000	1010	1010	0100	1011
	01	00		01	11	11	
00000	0000	0000	00000	0000	0000	0000	00000
01011	0111	0001	01100	0001	0001	0010	01010
0001	1010	1000	1110	0110	1001	1111	1010
	01	01		01	10	01	

00000	0000	0000	00000	0000	0000	0000	00000
01111	0100	0001	10001	0111	0100	0011	00111
0010	1110	1011	0100	1011	0101	1010	0101
	11	01		01	10	01	

Figure 6 Fourth Bit substituted with the XOR of M sequence and BPOF

The modified Fourier Transform after the substitution of the code (EX-OR of PN and BPOF) is as shown in figure 7.

11904	79.3881 382147 828+85 .944886 472614 2i	113.657 778858 472- 203.398 400448 378i	265.516 711590 291- 82.3703 579346 237i	395. 0093 0146 5237 - 294. 9858 5009 445i	250.194 604691 514+11 6.52750 655213 1i	- 94.19 84749 07084 - 54.84 20215 27105 1i	- 106.18728072 5886- 296.56240728 0562i
- 169.46 17962 80955- 172.76 19738 28826i	- 62.9139 162921 922- 157.929 855115 425i	- 165.432 127780 595- 91.3959 030700 218i	- 38.9617 758914 151- 94.2654 762857 916i	41.9 6305 1267 7076 - 78.4 8631 9370 3447 i	160.671 335142 706+12 8.92137 938860 4i	35.16 97510 96319 6+90. 39960 51309 016i	- 437.59651079 4002- 218.24365681 7133i
107.87 26645 249- 140.32 99264 17348i	- 81.8277 355912 678- 131.640 501700 676i	58.1678 811238 511- 59.2072 428471 512i	205.095 581524 419+11 4.72054 061570 9i	164. 7833 5630 1682 +37. 5159 3642 6445 2i	317.625 127341 672+38 .913731 267849 2i	16.07 86404 87362 9- 159.1 90066 65014 7i	- 165.69662767 3254+98.9627 585393171i
29.392 18503 72419 +22.47 44178 73140 4i	343.790 530128 937+28 .862976 174754 1i	8.90833 780926 303+6. 453023 901711 1i	201.107 992387 012+63 .848064 951613 1i	112. 2699 1238 3164 - 131. 6224 4023 523i	125.400 834414 869- 195.188 705431 576i	366.2 19240 42591 7- 213.6 80761 74954 2i	130.54012603 9018+151.523 184673889i
-214	130.540 126039 018- 151.523 184673 889i	366.219 240425 918+21 3.68076 174954 i	125.400 834414 87+195 .188705 431576 i	112. 2699 1238 3164 +131 .622 4402 3523 i	201.107 992387 012- 63.8480 649516 133i	8.908 33780 92630 5- 6.453 02390 17110 7i	343.79053012 8937- 28.862976174 7553i
29.392 18503 72418- 22.474 41787 31405i	- 165.696 627673 254- 98.9627 585393 167i	16.0786 404873 636+15 9.19006 665014 7i	317.625 127341 672- 38.9137 312678 5i	164. 7833 5630 1681 - 37.5 1593 6426	205.095 581524 418- 114.720 540615 71i	58.16 78811 23851 3+59. 20724 28471 51i	- 81.827735591 2668+131.640 501700676i

				4454 i			
107.87 26645 249+1 40.329 92641 7348i	- 437.596 510794 001+21 8.24365 681713 5i	35.1697 510963 197- 90.3996 051309 016i	160.671 335142 705- 128.921 379388 604i	41.9 6305 1267 7074 +78. 4863 1937 0344 8i	- 38.9617 758914 147+94 .265476 285791 8i	- 165.4 32127 78059 5+91. 39590 30700 227i	- 62.913916292 1917+157.929 855115425i
- 169.46 17962 80954 +172.7 61973 82882 7i	- 106.187 280725 885+29 6.56240 728056 2i	- 94.1984 749070 838+54 .842021 527105 6i	250.194 604691 514- 116.527 506552 131i	395. 0093 0146 5237 +294 .985 8500 9445 i	265.516 711590 291+82 .370357 934623 3i	113.6 57778 85847 3+203 .3984 00448 377i	79.388138214 7827- 85.944886472 6143i

Figure 7 Modified Fourier Coefficients with Fourth Bit modified.

The inverse Fourier Transform for the same is:

252	200	256	244	199	201	160	177
120	199	201	160	177	202	160	201
188	150	200	200	177	201	160	201
198	143	159	176	202	160	177	178
177	202	161	201	232	198	181	201
199	200	129	199	177	200	160	200
199	271	177	201	159	199	189	128
120	176	201	160	200	198	198	132

Figure 8 Modified (watermarked) pixel block of size 8X8.

The above figure gives the modified watermarked image block.

V. Watermark Detection

The bit sequence extracted from the fourth bit plane is operated bitwise XOR with BPOF to give the m sequence. This m sequence gives perfect cross correlation giving -1. This is the characteristic property of the m sequence and can be illustrated as follows:

For the calculation of the PN sequence correlation analysis, 0 is replaced by -1, thus giving a sequence of 1 and -1 and the sequence is known as chip rate.

The cross correlation of the extracted sequence with PN sequence generated through the same seed and same recurrence relation is given by:

Figure 3.10 Correlation Based Detection of Watermark

The mean square error of the above image block is 30. Also

PSNR = $20 \log[255*255/MSE]$ is 66.71918212.



VI. Selective Watermarking against cutting/cropping Attacks

The above watermarking scheme can be used to watermark the image considering the portions of the image of block size 8X8 as illustrated in figure below.

Figure 11 Original Grayscale image of Lena



Figure 3.12 Watermarked Image of Lena (magnified 400 times). Watermarked in 8X8 portion of image shown in black square

Thus, any given image can be watermarked at some pre specified places so that watermark can be detected and can be extracted with high probability.

Moreover, the watermark can be embedded on such portions of the image (such as shown in the figure 3.10 above), such that the probability of cutting or cropping effects can be minimized. This technique can be applied to watermark several bit planes of the image based on the number of bit planes modified.

Watermarking specific portions of the image, selectively, with pre specified number of bit provide significant improvement over traditional DFT based watermarking, with improvements in the error probability of several orders of magnitude for most typical scenarios. PN sequences and Spread Spectrum is currently used by many watermarking schemes as the information embedding (or modulation) technology. Results provided in Chapter 4 clearly indicate that this correlation based image watermarking using m sequences provides a much robust watermarking as compared to existing technique of BPOF only watermarking technique which is mostly used as fragile watermark technique for image tempering detection. The proposed watermarking technique can be readily applied to practically any watermarking technique currently using PN sequences, taking immediate advantage of the gains.

VII. Effect of Image resizing

Image interpolation provides one of the most basic technique for image resizing. Interpolation is useful when one needs to reduce the file size or increase the amount of image data sent at one time. With the image size reduced, the image quality does not have to be significantly reduced as well.

Interpolation also provides a way through which images are enlarged. There are many different types of interpolation methods, each resulting in a different look to the final picture. Thus, it is best if the quality, or visible distinction for each pixel, is retained throughout the enlargement process. Thus, one cannot simply have a number of pixels directly represent a single original pixel. this type of interpolation is not sufficient for commercial use. Conspicuous blocks of single color will be visible, and depending on size of enlargement, the original image will be unrecognizable. Older methods of linear interpolation somewhat addressed this problem. By finding a mean pixel value between neighboring pixels, one can be able to produce an effect of blurred edges and smoothed details. Bilinear re-sampling uses the values from the four surrounding pixels, and new pixel values are calculated by weighting the averages of the four closest pixels based on distance. The new pixel value is determined by calculating a weighted average of the four closest pixels (2x2 array) based on distance. However, bilinear interpolation seems to work better for image reduction rather than image enlargement. Linear interpolation methods are simple and it has been found that nonlinear methods are superior. Some non-linear interpolation methods include Bi-Cubic, Soft Directional, and non-linear interpolation through extended permutation filters. Bicubic interpolation uses the nearest sixteen pixels (4x4 array) based on distance, which produces a much better effect than linear interpolation. Most high-end image manipulation and viewing programs today have some sort of interpolation process used when resizing an image. Such include ACDSee, Adobe Photoshop, IfranView, and even Internet Explorer. They implement many commercial interpolation methods like Lanczos Interpolation, standard Kneson, and pxISmartScale.

(a) Nearest Neighbor Interpolation

The most basic form of interpolation is Nearest Neighbor Interpolation. In case of image enlargement, as the actual pixels are proportionally copied to their new locations, their position in relation to one another remains the same. Since the image is enlarged, filler pixels must be placed in between the actual pixels.

With the most basic nearest neighbor interpolation, the process is to just copy the exact same pixel values over to the filler pixel closest to the pixel. Consider the following figure 3.13.

22	28
16	30

o.	Pixel Values	FFT	Brightness Adjusted Pixels	FFT
1	24	361	27	409
2	15	-42.9789037926387-31.8348821071031i	18	-42.9789037926387-31.8348821071031i
3	26	18.857864376269+4.34314575050763i	29	18.857864376269+4.34314575050763i
4	19	-37.465218650608-10.7524330107325i	22	-37.465218650608-10.7524330107325i
5	35	47+6i	38	47+6i
6	16	-29.3632084741382-11.4975990147935i	19	-29.3632084741382-11.4975990147935i
7	30	47.1421356237309-15.6568542494924i	33	47.1421356237309-15.6568542494924i
8	21	-18.192669082615+59.4199518888359i	24	-18.192669082615+59.4199518888359i
9	56	53	59	53
10	19	-18.192669082615-59.4199518888359i	22	-18.192669082615-59.4199518888359i
11	9	47.142135623731+15.6568542494924i	12	47.142135623731+15.6568542494924i
12	28	-29.3632084741382+11.4975990147934i	31	-29.3632084741382+11.4975990147934i
13	12	47-6i	15	47-6i
14	24	-37.465218650608+10.7524330107325i	27	-37.465218650608+10.7524330107325i
15	15	18.8578643762691-4.3431457505076i	18	18.8578643762691-4.3431457505076i
16	12	-42.9789037926387+31.8348821071031i	15	-42.9789037926387+31.8348821071031i

Figure 13 A 4 Pixel Test Block

For nearest neighbor interpolation 4 times, the resultant is shown in fig 3.14.

22	22	28	28
22	22	28	28
16	16	30	30
16	16	30	30

Figure 14 Nearest Neighbor Interpolation Scaled Image (4 times scaled)

An image scaled as per nearest neighbor interpolation can be readily identified and techniques can be implemented in the detector for the detection of the watermark originally embedded in the watermarked non-scaled image.

(b) Linear Interpolation

A better algorithm than nearest neighbor that takes into account the gradual transition of pixel color values. By finding the means between two pixel values, the filler pixel is better suited for overall image enhancement.

Consider again the same figure 3.4 repeated for ready reference.

22	28
16	30

With Filler pixels, the resultant is as shown in figure 15.

22	P	28	P
P	P	P	P
16	P	30	P
P	P	P	P

Figure 15 Linear Interpolation Scaled Image (4 times scaled)

For every P, one has to calculate the mean of the surrounding pixels. Eventually, one will be able to calculate the mean for every P, even those that were originally surrounded by all P. In the above example, the value of P comes out to be $(22+28+16+30)/4$.

It turns out that our proposed one dimensional FFT technique for watermark embedding fails when the image is scaled through linear interpolation. Thus, in case of linear watermarking, the proposed scheme serves as a technique for fragile watermarking.

(c)Image Brightness

Consider an image portion as shown in figure 16

24	15	26	19
35	16	30	21
56	19	9	28
12	24	15	12

Figure 16 Test Block 4X4 Pixels

Consider again the same image portion with adjusted brightness factor x, shown in figure 3.16

24+x	15+x	26+x	19+x
35+x	16+x	30+x	21+x
56+x	19+x	9+x	28+x
12+x	24+x	15+x	12+x

Figure 17 Test Block 4X4 Pixels (brightness increased with factor x)

Let x be 3. The FFT of original and brightness adjusted image is compared in the following table.

TABLE 2 PROPERTY OF FFT FOR UNIFORM INCREMENT/DECREMENT IN PIXEL VALUES (ADJUSTED BRIGHTNESS)

It turns out that our algorithm for image watermarking is robust against image brightness adjustment.

This can be understood with the following property of FFT.

$$f(x) \rightarrow F(u)$$

$$f(x+a) \rightarrow F(u)e^{-jau}$$

It is clear from the above table that frequency components remain unchanged when brightness is uniformly increased in pixels. Therefore, as per the proposed scheme of embedding, the modified bits in FFT magnitudes remain unchanged leading to the reliable detection of watermark even in brightness adjusted image.

VIII. Conclusion

The Fourier Transform is an important image processing tool which is used to decompose an image into its sine and cosine components. The output of the transformation represents the image in the Fourier or frequency domain, while the input image is the spatial domain equivalent. In the Fourier domain image, each point represents a particular frequency contained in the spatial domain image.

The Fourier Transform is used in a wide range of applications, such as image analysis, image filtering, image reconstruction, image compression and image watermarking. FFT based watermarking is robust against various types of attacks.

One obvious result can be derived from figure 4.9 in context of PSNR is this that it achieves a good value as the image size is reduced in case of grayscale image. This result follows from the fact that for images of size 32X32, the neighborhood of a specific pixel contains the intensity in some constrained range only, thus yielding smaller values for Mean Square Error and correspondingly, better PSNR.

REFERENCES

- [1] Cox, M. Miller, and A. McKellips, "Watermarking as communications with side information," Proc. IEEE, vol. 87, pp. 1127-1141, July 2008.
- [2] B. Chen and G. Wornell, "Achievable performance of digital watermarking systems," in Proc. Int. Conf. Multimedia Comput. Syst., Florence, Italy, June 2007, pp. 13-18
- [3] G. Depovre, et al., "Improved Watermark Detection Reliability Using Filtering Before Correlation", IEEE International Conference on Image Processing, ICIP-98, Vol.1, pp.430-434.

- [4] M. Miller, I. Cox, and J. Bloom, "Informed embedding: Exploiting image and detector information during watermark insertion," in Proc.IEEE Int. Conf. Image Process., 2002.J.
- [5] Dittmann, A. Steinmetz, and R. Steinmetz, "Content-based digital signature for motion pictures authentication and content-fragile watermarking," in IEEE Int. Conf. on Multimedia Computing and Systems, Vol. 2, pp. 209–213 2011.
- [6] F. Prez-Gonzlez, F. Balado, and J. R. Hernandez, Performance Analysis of Existing and New Methods for Data Hiding with Known-Host Information in Additive Channels, IEEE Trans. Signal Processing, vol. 51(4), pp. 960{980, April, 2012.
- [7] S.P.Mohanty, et al., "A Dual Watermarking Technique for Images", Proc. 7th ACM International Multimedia Conference, ACM-MM'99, Part 2, pp. 49-51, Orlando, USA, Oct. 2005.
- [8] I.J.Cox et. al., "Secure Spread Spectrum Watermarking of Images, Audio and Video", Proc IEEE International Conf on Image Processing, ICIP-96, Vol.3, pp 243-246, <http://www.neci.nj.nec.com/tr/neci tr 95 10.ps>
- [9] B. Javidi and E. Ahouzi, "Optical security system with Fourier plane encoding," Appl. Opt. 37~26, 6247–6255 ~2008.
- [10] Krishnan, N. Selvakumar, R.K. Rajapandian, S. Arul Mozhi, K. Nelson, Kennedy Babu, "A Wavelet Transform Based Digital Image Watermarking and Authentication", Annual IEEE Conference, in India, 15-17 Sept. 2006, pp: 1-6
- [11] H. Malik, A. Khokhar, and R. Ansari, An Improved Detector/Decoder for Spread Spectrum based Watermarking using Independent Component Analysis, ACM Fifth Workshop on Digital Rights Management (DRM'05), November 7, 2005.
- [12] J.R.Smith and B.O.Comiskey, "Modulation and Information Hiding in Images", Proc. of First International Workshop on Information Hiding, University of Canbridge, UK, May 30-June 1 1996, Lecture Notes in Comp. Sc., Vol.1174, Ross Anderson (Ed.).
- [13] Abu-Errub, A., Al-Haj, A.,"Optimized DWT-based image watermarking", First International Conference on Applications of Digital Information and Web Technologies, IEEE,2008, 4-6.
- [14] D. Kirovski and H. Malvar, "Robust spread-spectrum audio watermarking," in Proc. Int. Conf. Acoust., Speech, Signal Process., Salt Lake City, UT, May 2001.
- [15] Cichocki, S. Douglas, and S. Amari, Robust Techniques for Independent Component Analysis (ICA) with Noisy Data, Neurocomputing, Elsevier Science, vol. 22, pp. 113{129, 2001.
- [16] Ahmad Nilchi1, Ayoub Taher," A New Robust Digital Image Watermarking Technique based on the Discrete Cosine Transform and Neural Network", pp:1 – 7, April 2008.
- [17] Abu-Errub, A., Al-Haj, A.,"Optimized DWT-based image watermarking", First International Conference on Applications of Digital Information and Web Technologies, IEEE,2008, 4-6. J.J.K. O'Ruanaidh, et al., "Phase Watermarking on Digital Images", Proc. IEEE International Conf. on Image Processing, ICIP-96, Vol.3, pp 239-242.
- [18] R. Gribonval, L. Benaroya, E. Vincent, C. Fvotte, Proposals for Performance Measurement in Source Separation, 4th Int. Sym. Independent Component Analysis and Blind Source Separation (ICA'03), April, 2003.
- [19] K.Hill, "A Perspective: The Role of Identifiers in Managing and Protecting Intellectual Property in the Digital Age", Proceedings of the IEEE, Vol.87, No.7, July 2009, pp.1228-1238.
- [20] M.D.Swanson, et al., "Multimedia data Embedding and Watermarking Technologies", Proc. of the IEEE, Vol.86, No.6, June 2006, pp.1064-1087.
- [21] S.Craver, "On Public-Key Steganography in the Presence of an Active Warden", Proc. of the 2nd International Workshop on Information Hiding, Portland, Oregon, USA, 15-17 Apr 1998, Lecture notes in Comp Sc, Vol.1525, Springer-Verlag.
- [22] Z. Tirkel, C. F. Osborne, and R. G. van Schyndel, "Image watermarking—A spread spectrum application," in Proc. IEEE 4th Int. Symp. Spread Spectrum Techn. Applicat., Mainz, Germany, 2006, pp. 785–789
- [23] J. Fridrich and M. Goljan, "Images with self-correcting capabilities," in Proc. Int. Conf. on Image Processing, Vol. 3, pp. 792–796 ~2005.