



Hesitant Fuzzy Linguistic Term Set Based Laws of Algebra of Sets

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Abstract—This Paper Presents Hesitant Fuzzy Information About Data Sets. Hesitant Fuzzy Linguistic Term Set (HFLT) is based on the fuzzy linguistic Approach that will serve as basis to Increase the flexibility of elicitation of linguistic Information. For experimental Classification accuracy results analysis evaluated using the Analytical SAS 9.0 Software is used. The Experimental Laws of Algebra Results show the proposed approach Best performs.

Keywords— Hesitant Fuzzy Set, Laws of Algebra, Data sets, Linguistic Term Set.

I. INTRODUCTION

Hesitant Fuzzy Information collection based on Fuzzy logic, Fuzzy sets theory, Intuitionistic fuzzy sets, Fuzzy multi sets, fuzzy linguistic approach, uncertainty and model the information etc. In this Paper Hesitant Fuzzy Linguistic Term Set (HFLT) is used to calculating Document Classification Results.

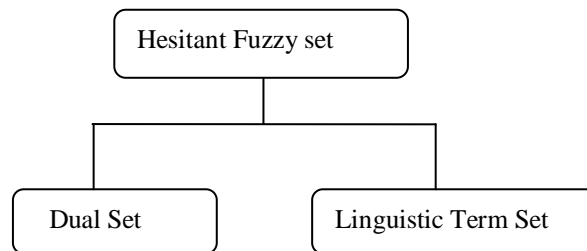


Fig 1: Hesitant Fuzzy Information collection

H. Becker, "Computing with words and machine learning in medical diagnosis[2], Y. Dong, Y. Xu, and S. Yu, "Computing the numerical scale of the linguistic term set for the 2-tuple fuzzy linguistic representation model[5]. D. Dubois and H. Prade, Fuzzy Sets and Systems: Theory and Applications [6]. Z. P. Fan, J. Ma, and Q. Zhang, "An approach to multiple attribute decision making based on fuzzy preference information alternatives[7], D. F. Li, "TOPSIS-based nonlinear-programming methodology for multi attribute decision making with interval-valued intuitionistic fuzzy sets[18].

F. Herrera, E. Herrera-Viedma, and L. Mart'inez, "A fusion approach for managing multi-granularity linguistic terms sets in decision making[10], F. Herrera and L. Mart'inez, "A 2-tuple fuzzy linguistic representation model for computing with words[12]. S. Kundu, "Min-transitivity of fuzzy leftness relationship and its application to decision making [16], H. Ishibuchi and H. Tanaka, "Theory and methodology: Multi objective programming in optimization of the interval objective function [14]. G. Bordogna and G. Pasi, "A fuzzy linguistic approach generalizing Boolean information retrieval: A model and its evaluation[4], J. Kacprzyk and S. Zadrozny, "Computing with words is an implementable paradigm: Fuzzy queries, linguistic data summaries, and natural-language generation[15], H. Ishibuchi, T. Nakashima, and M. Nii, Classification and Modelling With Linguistic Information Granules: Advanced Approaches to Linguistic Data Mining [13], D. F. Li, "Multi attribute group decision making method using extended linguistic variables[17].

P. P. Bonissone, "A fuzzy sets based linguistic approach: Theory and applications [3], J. Ma, D. Ruan, Y. Xu, and G. Zhang, "A fuzzy-set approach to treat determinacy and consistency of linguistic terms in multi-criteria decision making[19], F. Herrera, E. Herrera-Viedma, and L. Mart'inez, "A fuzzy linguistic methodology to deal with unbalanced linguistic term sets[11], L. Mart'inez, "Sensory evaluation based on linguistic decision analysis[20].

K.T. Atanassov, "Intuitionistic fuzzy sets[1], J.M. Garibaldi, M. Jaroszewski, and S. Musikasuwan, "Nonstationary fuzzy sets [8], F. Herrera, S. Alonso, F. Chiclana, and E. Herrera-Viedma, "Computing with words in decision making: Foundations, trends and prospects[9], Computing Vectors Based Document Clustering and Numerical Result Analysis[22], Hesitant Distance Similarity Measures for Document Clustering[21], Hesitant k-Nearest Neighbor (HK- nn) Classifier for Document Classification and Numerical Result Analysis[23].

The paper is organized as follows. Section-I described the introduction and review of literatures. In Section-II, the Hesitant Fuzzy Information is described. In Section-III, Methodology of document Classification accuracy results is described. In Section-IV, Experimental results are described. In Section-V, Evaluation measurement is described. Finally, we concluded and proposed some future directions in Conclusion Section.

II. HESITANT FUZZY LINGUISTIC TERM SET

Hesitant Fuzzy Linguistic Term Set: Uncertainty is a problem that occurs when calculating document classification results then the best and optimum solution in present time is given by Hesitant Fuzzy Set. Hesitant Fuzzy Set gives new computational solution with numerical capability. Hesitant Fuzzy used Linguistic Term Set then it knows Hesitant Fuzzy Linguistic Term Set (HFLT). Linguistic Term Set just like Context Free Grammar (CFG).

A. Theorem 1: (Idempotent laws)

For any Hesitant Fuzzy Linguistic Term Set H_s , we have (i) $H_s \cup H_s = H_s$ (ii) $H_s \cap H_s = H_s$

(i) proof $H_s \cup H_s = \{x: x \in H_s \text{ or } x \in H_s\} = \{x: x \in H_s\} = H_s$

(ii) proof $H_s \cap H_s = \{x: x \in H_s \text{ and } x \in H_s\} = \{x: x \in H_s\} = H_s$

B. Theorem 2: (Identity laws)

For any Hesitant Fuzzy Linguistic Term Set H_s , we have (i) $H_s \cup \phi = H_s$ (ii) $H_s \cap \mu = H_s$, ϕ, μ are identity elements

for union and intersection respectively.

(i) proof $H_s \cup \phi = \{x: x \in H_s \text{ or } x \in \phi\} = \{x: x \in H_s\} = H_s$

(ii) proof $H_s \cap \mu = \{x: x \in H_s \text{ and } x \in \mu\} = \{x: x \in H_s\} = H_s$

C. Theorem 3: (Commutative laws)

For any two Hesitant Fuzzy Linguistic Term Set H_s and H_s^1 , we have (i) $H_s \cup H_s^1 = H_s^1 \cup H_s$

(ii) $H_s \cap H_s^1 = H_s^1 \cap H_s$ Union and intersection are commutative.

(i) Proof: Let x be an arbitrary element of $H_s \cup H_s^1$ Then,

$$x \in H_s \cup H_s^1 \Rightarrow x \in H_s \text{ or } x \in H_s^1 \Rightarrow x \in H_s^1 \text{ or } x \in H_s \Rightarrow x \in H_s^1 \cup H_s$$

$$H_s \cup H_s^1 \subseteq H_s^1 \cup H_s \dots 1$$

Let x be an arbitrary element of $H_s^1 \cup H_s$ Then,

$$x \in H_s^1 \cup H_s \Rightarrow x \in H_s^1 \text{ or } x \in H_s \Rightarrow x \in H_s \text{ or } x \in H_s^1 \Rightarrow x \in H_s \cup H_s^1$$

$$H_s^1 \cup H_s \subseteq H_s \cup H_s^1 \dots 2$$

Hence, from 1 and 2

$$H_s \cup H_s^1 = H_s^1 \cup H_s$$

(ii) Proof: Let x be an arbitrary element of $H_s \cap H_s^1$ Then,

$$x \in H_s \cap H_s^1 \Rightarrow x \in H_s \text{ and } x \in H_s^1 \Rightarrow x \in H_s^1 \text{ and } x \in H_s \Rightarrow x \in H_s^1 \cap H_s$$

$$H_s \cap H_s^1 \subseteq H_s^1 \cap H_s \dots 3$$

Let x be an arbitrary element of $H_s^1 \cap H_s$ Then,

$$x \in H_s^1 \cap H_s \Rightarrow x \in H_s^1 \text{ and } x \in H_s \Rightarrow x \in H_s \text{ and } x \in H_s^1 \Rightarrow x \in H_s \cap H_s^1$$

$$H_s^1 \cap H_s \subseteq H_s \cap H_s^1 \dots 4$$

Hence, from 3 and 4

$$H_s \cap H_s^1 = H_s^1 \cap H_s$$

D. Theorem 4: (Associative laws)

If any H_s , H_s^1 and H_s^2 , are three Hesitant Fuzzy Linguistic Term Set then

$$(i) (H_s \cup H_s^1) \cup H_s^2 = H_s \cup (H_s^1 \cup H_s^2) \quad (ii) H_s \cap (H_s^1 \cap H_s^2) = (H_s \cap H_s^1) \cap H_s^2$$

Union and intersection are associative.

(i) Proof : Let x be an arbitrary element of $(H_s \cup H_s^1) \cup H_s^2$ Then

$$x \in (H_s \cup H_s^1) \cup H_s^2 \Rightarrow x \in (H_s \cup H_s^1) \text{ or } x \in H_s^2 \Rightarrow (x \in H_s \text{ or } x \in H_s^1) \text{ or } x \in H_s^2 \Rightarrow x \in H_s \text{ or } (x \in H_s^1 \text{ or } x \in H_s^2)$$

$$\Rightarrow x \in H_s \text{ or } x \in (H_s^1 \cup H_s^2) \Rightarrow x \in H_s \cup (H_s^1 \cup H_s^2)$$

$$(H_s \cup H_s^1) \cup H_s^2 \subseteq H_s \cup (H_s^1 \cup H_s^2) \dots 5$$

Let x be an arbitrary element of $H_s \cup (H_s^1 \cup H_s^2)$ Then

$$x \in H_s \cup (H_s^1 \cup H_s^2) \Rightarrow x \in H_s \text{ or } x \in (H_s^1 \cup H_s^2) \Rightarrow x \in H_s \text{ or } (x \in H_s^1 \text{ or } x \in H_s^2) \Rightarrow (x \in H_s \text{ or } x \in H_s^1) \text{ or } x \in H_s^2$$

$$\Rightarrow x \in (H_s \cup H_s^1) \text{ or } x \in H_s^2 \Rightarrow x \in (H_s \cup H_s^1) \cup H_s^2$$

$$H_s \cup (H_s^1 \cup H_s^2) \subseteq (H_s \cup H_s^1) \cup H_s^2 \dots 6$$

Hence, from 5 and 6

$$(H_s \cup H_s^1) \cup H_s^2 = H_s \cup (H_s^1 \cup H_s^2)$$

(ii) Proof: Let x be an arbitrary element of $H_s \cap (H_s^1 \cap H_s^2)$ Then

$$x \in H_s \cap (H_s^1 \cap H_s^2) \Rightarrow x \in H_s \text{ and } x \in (H_s^1 \cap H_s^2) \Rightarrow x \in H_s \text{ and } (x \in H_s^1 \text{ and } x \in H_s^2) \Rightarrow (x \in H_s \text{ and } x \in H_s^1) \text{ and } x \in H_s^2$$

$$\Rightarrow x \in (H_s \cap H_s^1) \text{ and } x \in H_s^2 \Rightarrow x \in (H_s \cap H_s^1) \cap H_s^2$$

$$H_s \cap (H_s^1 \cap H_s^2) \subseteq (H_s \cap H_s^1) \cap H_s^2 \dots 7$$

Let x be an arbitrary element of $(H_s \cap H_s^1) \cap H_s^2$ Then

$$x \in (H_s \cap H_s^1) \cap H_s^2 \Rightarrow x \in (H_s \cap H_s^1) \text{ and } x \in H_s^2 \Rightarrow (x \in H_s \text{ and } x \in H_s^1) \text{ and } x \in H_s^2 \Rightarrow x \in H_s \text{ and } (x \in H_s^1 \text{ and } x \in H_s^2)$$

$$\Rightarrow x \in H_s \text{ and } x \in (H_s^1 \cap H_s^2) \Rightarrow x \in H_s \cap (H_s^1 \cap H_s^2)$$

$$(H_s \cap H_s^1) \cap H_s^2 \subseteq H_s \cap (H_s^1 \cap H_s^2) \dots 8$$

Hence, from 7 and 8

$$H_s \cap (H_s^1 \cap H_s^2) = (H_s \cap H_s^1) \cap H_s^2$$

E. Theorem 5: (Distributive laws)

If any H_s, H_s^1 and H_s^2 are three Hesitant Fuzzy Linguistic Term Set

$$(i) H_s \cup (H_s^1 \cap H_s^2) = (H_s \cup H_s^1) \cap (H_s \cup H_s^2) \quad (ii) H_s \cap (H_s^1 \cup H_s^2) = (H_s \cap H_s^1) \cup (H_s \cap H_s^2)$$

Union and intersection are distributive over intersection and union respectively.

(i) Proof: Let x be an arbitrary element of $H_s \cup (H_s^1 \cap H_s^2)$ Then

$$x \in H_s \cup (H_s^1 \cap H_s^2) \Rightarrow x \in H_s \text{ or } x \in (H_s^1 \cap H_s^2) \Rightarrow x \in H_s \text{ or } (x \in H_s^1 \text{ and } x \in H_s^2) \Rightarrow (x \in H_s \text{ or } x \in H_s^1) \text{ and } (x \in H_s \text{ or } x \in H_s^2)$$

['or' is distributive over 'and']

$$\Rightarrow x \in (H_s \cup H_s^1) \text{ and } x \in (H_s \cup H_s^2) \Rightarrow x \in (H_s \cup H_s^1) \cap (H_s \cup H_s^2)$$

$$H_s \cup (H_s^1 \cap H_s^2) \subseteq (H_s \cup H_s^1) \cap (H_s \cup H_s^2) \dots 9$$

Let x be an arbitrary element of $(H_s \cup H_s^1) \cap (H_s \cup H_s^2)$ Then

$$x \in (H_s \cup H_s^1) \cap (H_s \cup H_s^2) \Rightarrow x \in (H_s \cup H_s^1) \text{ and } x \in (H_s \cup H_s^2) \Rightarrow (x \in H_s \text{ or } x \in H_s^1) \text{ and } (x \in H_s \text{ or } x \in H_s^2)$$

$$\Rightarrow x \in H_s \text{ or } (x \in H_s^1 \text{ and } x \in H_s^2) \Rightarrow x \in H_s \cup (H_s^1 \cap H_s^2)$$

$$(H_s \cup H_s^1) \cap (H_s \cup H_s^2) \subseteq H_s \cup (H_s^1 \cap H_s^2) \dots 10$$

Hence, from 9 and 10

$$H_s \cup (H_s^1 \cap H_s^2) = (H_s \cup H_s^1) \cap (H_s \cup H_s^2)$$

(ii) Proof: Let x be an arbitrary element of $H_s \cap (H_s^1 \cup H_s^2)$ Then

$$x \in H_s \cap (H_s^1 \cup H_s^2) \Rightarrow x \in H_s \text{ and } x \in (H_s^1 \cup H_s^2) \Rightarrow x \in H_s \text{ and } (x \in H_s^1 \text{ or } x \in H_s^2) \Rightarrow (x \in H_s \text{ and } x \in H_s^1) \text{ or } (x \in H_s \text{ and } x \in H_s^2)$$

$$\Rightarrow x \in (H_s \cap H_s^1) \text{ or } x \in (H_s \cap H_s^2) \Rightarrow x \in (H_s \cap H_s^1) \cup (H_s \cap H_s^2)$$

$$H_s \cap (H_s^1 \cup H_s^2) \subseteq (H_s \cap H_s^1) \cup (H_s \cap H_s^2) \dots 11$$

Let x be an arbitrary element of $(H_s \cap H_s^1) \cup (H_s \cap H_s^2)$ Then

$$\Rightarrow x \in (H_s \cap H_s^1) \cup (H_s \cap H_s^2) \Rightarrow x \in (H_s \cap H_s^1) \text{ or } x \in (H_s \cap H_s^2) \Rightarrow (x \in H_s \text{ and } x \in H_s^1) \text{ or } (x \in H_s \text{ and } x \in H_s^2)$$

$$\Rightarrow x \in H_s \text{ and } (x \in H_s^1 \text{ or } x \in H_s^2) \Rightarrow x \in H_s \cap (H_s^1 \cup H_s^2)$$

$$(H_s \cap H_s^1) \cup (H_s \cap H_s^2) \subseteq H_s \cap (H_s^1 \cup H_s^2) \dots 12$$

Hence, from 11 and 12

$$H_s \cap (H_s^1 \cup H_s^2) = (H_s \cap H_s^1) \cup (H_s \cap H_s^2)$$

Theorem 6: (De-Morgan's laws)

If any H_s, H_s^1 are two Hesitant Fuzzy Linguistic Term Set then

$$(i) (H_s \cup H_s^1)' = H_s' \cap H_s^{1'} \quad (ii) (H_s \cap H_s^1)' = H_s' \cup H_s^{1'}$$

(i) Proof: Let x be an arbitrary element of $(H_s \cup H_s^1)'$ Then

$$x \in (H_s \cup H_s^1)' \Rightarrow x \notin (H_s \cup H_s^1) \Rightarrow x \notin H_s \text{ and } x \notin H_s^1$$

$$\Rightarrow x \in H_s' \text{ and } x \in H_s^{1'} \Rightarrow x \in H_s' \cap H_s^{1'}$$

$$(H_s \cup H_s^1)' \subseteq H_s' \cap H_s^{1'} \dots 13$$

Let y be an arbitrary element of $H_s' \cap H_s^{1'}$, then

$$\Rightarrow y \in H_s' \cap H_s^{1'} \Rightarrow y \in H_s' \text{ and } y \in H_s^{1'} \Rightarrow y \notin H_s \text{ and } y \notin H_s^1$$

$$\Rightarrow y \notin H_s \cup H_s^1 \Rightarrow y \in (H_s \cup H_s^1)'$$

$$H'_s \cap H_s^1 \subseteq (H_s \cup H_s^1)' \dots 14$$

Hence, from 13 and 14

$$(H_s \cup H_s^1)' = H'_s \cap H_s^1$$

(ii) Proof : Let x be an arbitrary element of $(H_s \cap H_s^1)'$. Then

$$x \in (H_s \cap H_s^1)' \Rightarrow x \notin (H_s \cap H_s^1) \Rightarrow x \notin H_s \text{ or } x \notin H_s^1$$

$$\Rightarrow x \in H'_s \text{ or } x \in H_s^1 \Rightarrow x \in H'_s \cup H_s^1$$

$$(H_s \cap H_s^1)' \subseteq H'_s \cup H_s^1 \dots 15$$

Let y be an arbitrary element of $H'_s \cup H_s^1$, then

$$y \in (H'_s \cup H_s^1) \Rightarrow y \in H'_s \text{ or } y \in H_s^1 \Rightarrow y \notin H_s \text{ or } y \in H_s^1 \Rightarrow y \notin (H_s \cap H_s^1)$$

$$\Rightarrow y \in (H_s \cap H_s^1)' \quad H'_s \cup H_s^1 \subseteq (H_s \cap H_s^1)' \dots 16$$

Hence, from 15 and 16

$$(H_s \cap H_s^1)' = H'_s \cup H_s^1$$

III. METHODOLOGY

In the Classification of document different the steps are used. The steps are as follows:

- A. *Data Collection*: In this phase collect relevant documents like e-mail, news, web pages etc. from various heterogeneous sources. These text documents are stored in a variety of formats depending on the nature of the data. The datasets are downloaded from UCI KDD Archive. This is an online repository of large datasets and has wide variety of data types.
- B. *Classification Method*: Initial step is to complete review of literature in the field of data mining. Next step is a detailed survey of data mining and existing Algorithms for Classification. In this area some work done by various researchers. After studying their work, it would be attempted to find the Classification algorithm.
- C. *Classification Process*: Algorithms develop for Classification Process. Classification Process means transform documents into a suitable determined in classes for the Classification task. In Classification Process we performed Different tasks. Optimized classification will also be studied. The real data may be great source for the Classification.

D. *Classification Results:* In this Experiment we calculate Hesitant Fuzzy Linguistic Term Set Based Document Classification. Hesitant Fuzzy Linguistic Term Set Based Document Classification is efficient and accurate compare to other Classification method.

IV. EXPERIMENTAL RESULTS

In this Experiment we calculate Hesitant Fuzzy Linguistic Term Set (HFLT) based accuracy percentage for laws of Algebra of Sets.

TABLE I
ACCURACY PERCENTAGE OF LAWS OF ALGEBRA OF SETS

| | Idempotent | Identity | Commutative | Associative | Distributive | De-Morgan |
|-------|-------------------|-----------------|--------------------|--------------------|---------------------|------------------|
| 500 | 0.85 | 0.98 | 0.94 | 0.97 | 0.82 | 0.98 |
| 1000 | 0.83 | 0.95 | 0.91 | 0.85 | 0.78 | 0.95 |
| 2000 | 0.81 | 0.93 | 0.89 | 0.83 | 0.75 | 0.93 |
| 3500 | 0.68 | 0.92 | 0.88 | 0.78 | 0.74 | 0.92 |
| 5000 | 0.78 | 0.89 | 0.87 | 0.75 | 0.74 | 0.89 |
| 6500 | 0.76 | 0.87 | 0.85 | 0.74 | 0.73 | 0.87 |
| 8000 | 0.74 | 0.85 | 0.82 | 0.74 | 0.73 | 0.85 |
| 10000 | 0.72 | 0.83 | 0.81 | 0.73 | 0.73 | 0.83 |

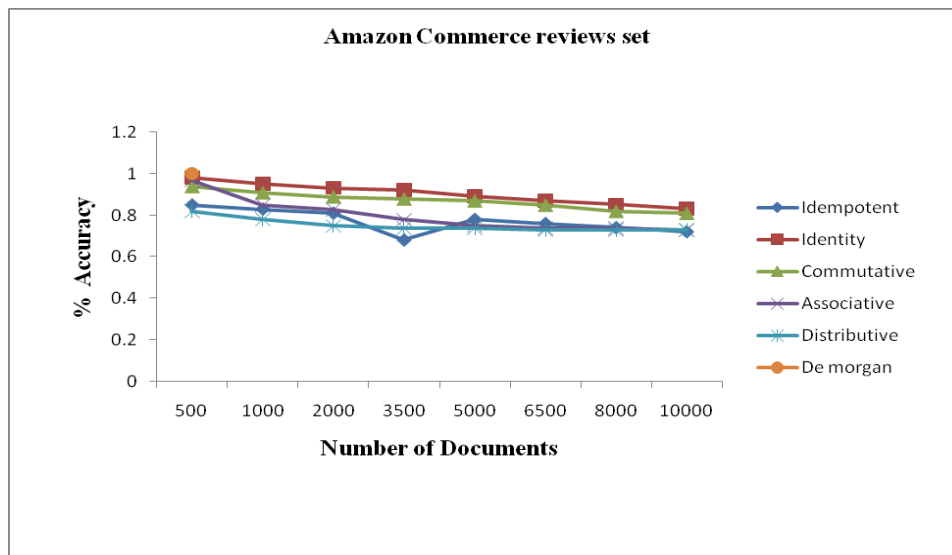


Fig. 2 Accuracy percentages of Laws of Algebra of Sets

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