



Radon Transform and Symbolic PCA based 3D Face Recognition using KNN and SVM

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Abstract— In spite of over two decades of intense research, illumination and pose invariance remain prohibitively challenging aspects of face recognition for most practical application. Automatic face recognition has long been established as one of the most active research areas in computer vision. In spite of the large number of developed algorithms, real-world performance of state-of-the-art methods has been disappointing. Three-dimensional face recognition (3D face recognition) is a modality of facial recognition methods in which the three-dimensional geometry of the human face is used. It has been shown that 3D face recognition methods can achieve significantly higher accuracy than their 2D counterpart. A 3D face image is represented by 3D meshes or range images which contain depth information. In the literature, there are several methods for face recognition using range images, which are focused on the data acquisition and pre-processing stage only. In this paper, we proposed a new method based on Radon transform and Symbolic PCA for face recognition using 3D range images. The experimentation has been done using three face databases, namely, Bosphorus 3D face database, Texas 3D face database and CASIA 3D face database. The experimental results show that the proposed algorithm performs satisfactorily with an average accuracy of 98.00% for SVM classifier and is efficient in terms of accuracy and detection time.

Keywords— 3D face recognition, radon transform, symbolic PCA, KNN, SVM.

I. INTRODUCTION

Biometrics refers to the identification of humans by their characteristics or traits. Biometrics is used in computer science as a form of identification and access control. It is also used to identify individuals in groups that are under surveillance. Many different aspects of human physiology, chemistry or behaviour can be used for biometric authentication. The selection of a particular biometric for use in a specific application involves a weighting of several factors. A number of biometric traits have been developed and are used to authenticate the person's identity. The idea is to use the special characteristics of a person to identify him. By using special characteristics we mean the using the features such as face, iris, fingerprint, signature etc. The method of identification based on biometric characteristics is preferred over traditional passwords and PIN based methods for various reasons such as: The person to be identified is required to be physically present at the time-of-identification. Identification based on biometric techniques obviates the need to remember a password or carry a token. A biometric system is essentially a pattern recognition system which makes a personal identification by determining the authenticity of a specific physiological or behavioural characteristic possessed by the user. A biometric system can be either an 'identification' system or a 'verification' (authentication) system.

Human face images are useful not only for person recognition, but for also revealing other attributes like gender, age, ethnicity, and emotional state of a person. Therefore, face is an important biometric identifier in the law enforcement and human computer interaction (HCI) communities. Detecting faces in a given image and recognizing persons based on their face images are classical object recognition problems that have received extensive attention in the computer vision literature. While humans are perceived to be good at recognizing familiar faces, the exact cognitive processes involved in this activity are not well understood. Therefore, training a machine to recognize faces as humans do is an arduous task. However, general methods used in object recognition such as appearance based, model based, and texture based approaches are also applicable to the specific problem of face detection and recognition.

The face is the frontal portion of the human head, extending from the forehead to the chin and includes the mouth, nose, cheeks, and eyes. Being the foremost part in one's interactions with the outer world, the face houses most of the fundamental sensory organs necessary for perceiving the world around, namely, eyes for seeing, nose for smelling, mouth for tasting, and ears for hearing. The face is considered to be the most commonly used biometric trait by humans; we recognize each other and, in many cases, establish our identities based on faces. Hence, it has become a standard practice to incorporate face photographs in various tokens of authentication such as ID cards, passports, and driver's licenses. Face Recognition and verification have been at the top of the research agenda of the computer vision community for more than a decade. The scientific interest in this research topic has been motivated by several factors. The main attractor is the inherent challenge that the problem of face image processing, face detection and recognition. However, the impetus for better understanding of the issues raised by automatic face recognition is also fuelled by the

immense commercial significance that robust and reliable face recognition technology would entail. Its applications are envisaged in physical and logical access control, security, man-machine interfaces and low bitrate communication.

To date, most of the research efforts, as well as commercial developments, have focused on two dimensional (2D) approaches. This focus on monocular imaging has partly been motivated by costs but to a certain extent also by the need to retrieve faces from existing 2D image and video database. With recent advances in image capture techniques and devices, various types of face-image data have been utilized and various algorithms have been developed for each type of image data. Among various types of face images, a 2D intensity image has been the most popular and common image data used for face recognition because it is easy to acquire and utilize. It, however, has the intrinsic problem that it is vulnerable to the change of illumination. Sometimes the change of illumination gives more difference than the change of people, which severely degrades the recognition performance. Therefore, illumination-controlled images are required to avoid such an undesirable situation when 2D intensity images are used. To overcome the limitation of 2D intensity images, Three Dimensional (3D) images are being used, such as 3D meshes and range images. A 3D mesh image is the best 2D representation of 3D objects. It contains 3D structural information of the surface as well as the intensity information of each point. By utilizing the 3D structural information, the problem of vulnerability to the change of illumination can be solved. A 3D mesh image is suitable image data for face recognition, but it is complex and difficult to handle.

A range image is simply an image with depth information. In other words, a range image is an array of numbers where the numbers quantify the distances from the focal plane of the sensor to the surfaces of objects within the field of view along rays emanating from a regularly spaced grid. Range images have some advantages over 2D intensity images and 3D mesh images. First, range images are robust to the change of illumination and color because the value on each point represents the depth value which does not depend on illumination or color. Also, range images are simple representations of 3D information. The 3D information in 3D mesh images is useful in face recognition, but it is difficult to handle. Different from 3D mesh images, it is easy to utilize the 3D information of range images because the 3D information of each point is explicit on a regularly spaced grid. Due to these advantages, range images are very promising in face recognition.

The majority of the 3D face recognition studies have focused on developing holistic statistical techniques based on the appearance of face range images or on techniques that employ 3D surface matching. A survey of literature on the research work focusing on various potential problems and challenges in the 3D face recognition can be found in the survey[1-5]. Gupta et al.[6] presented a novel anthropometric 3D face recognition algorithm. This approach employs 3D Euclidean and Geodesic distances between 10 automatically located anthropometric facial fiducial points and a linear discriminant classifier with 96.8% recognition rate. Lu et al.[7] constructed many 3D models as registered templates, then they matched 2.5D images (original 3D data) to these models using iterative closest point (ICP). Chang et al. [8] describe a "multi-region" approach to 3D face recognition. It is a type of classifier ensemble approach in which multiple overlapping sub regions around the nose are independently matched using ICP and the results of the 3D matching are fused. Jahanbim et al. [9] presented an approach of verification system based on Gabor features extracted from range images. In this approach, multiple landmarks (fiducials) on face are automatically detected, and also the Gabor features on all fiducials are concatenated, to form a feature vector to collect all the face features. Hiremath et al.[18] have discussed the 3D face recognition by using Radon Transform and PCA with recognition accuracy of 95.30%. Hengliand Tang et al.[19] presented a 3D face recognition algorithm based on sparse representation. In this method they used geometrical features, namely, triangle area, triangle normal and geodesic distance.

In this paper, our objective is to propose Radon transform and Symbolic PCA based 3D face recognition. The experimentation is carried out using three publicly available databases, namely, Bosphorus, Texas and CASIA 3D face databases.

II. MATERIALS AND METHODS

For purpose of experimentation of the proposed methodology, the face images drawn from the following 3D face databases are considered: (i) Bosphorus 3D face database, (ii) Texas 3D face database, (iii) CASIA 3D face database.

A. Bosphorus 3D Face Database

The Bosphorus 3D face database consists of 105 subjects in various poses, expressions and occlusion conditions. The 18 subjects have beard/moustache and the 15 subjects have hair. The majority of the subjects are aged between 25 and 35. There are 60 men and 45 women in total, and most of the subjects are Caucasian. Two types of expressions have been considered in the Bosphorus database. In the first set, the expressions are based on action units. In the second set, facial expressions corresponding to certain emotional expressions are collected. These are: happiness, surprise, fear, sadness, anger and disgust.

The facial data are acquired using Inspeck Mega Capturor II 3D, which is a commercial structured-light based 3D digitizer device. The sensor resolution in x, y & z (depth) dimensions are 0.3mm, 0.3mm and 0.4mm respectively, and colour texture images are high resolution (1600x1200 pixels). It is able to capture a face in less than a second. Subjects were made to sit at a distance of about 1.5 meters away from the 3D digitizer. A 1000W halogen lamp was used in a dark room to obtain homogeneous lighting. However, due to the strong lighting of this lamp and the device's projector, usually specular reflections occur on the face. This does not only affect the texture image of the face but can also cause noise in the 3D data. To prevent it, a special powder which does not change the skin colour is applied to the subject's face. Moreover, during acquisition, each subject wore a band to keep his/her hair above the forehead to prevent hair

occlusion, and also to simplify the face segmentation task. The propriety software of the scanner is used for acquisition and 3D model reconstruction[10].

B. Texas 3D Face Database

The Texas 3D Face Recognition (Texas 3DFR) database is a collection of 1149 pairs of facial color and range images of 105 adult human subjects. These images were acquired using a stereo imaging system manufactured by 3Q Technologies (Atlanta, GA) at a very high spatial resolution of 0.32 mm along the x, y, and z dimensions. During each acquisition, the color and range images were captured simultaneously and thus the two are perfectly registered to each other. This large database of two 2D and 3D facial models was acquired at the company Advanced Digital Imaging Research (ADIR), LLC (Friendswood, TX), formerly a subsidiary of Iris International, Inc. (Chatsworth, CA), with assistance from research students and faculty from the Laboratory for Image and Video Engineering (LIVE) at The University of Texas at Austin. This project was sponsored by the Advanced Technology Program of the National Institute of Standards and Technology (NIST). Texas 3DFRD was created to develop and test 3D face recognition algorithms intended to operate in environments with cooperative subjects, wherein, the faces are imaged in a relatively fixed position and distance from the camera [11].

C. CASIA 3D Face Database

CASIA 3D Face Database consisting of 4624 scans of 123 persons using the non-contact 3D digitizer, Minolta Vivid 910. During building the database, not only the single variations of poses, but also expressions and illuminations are considered [12].

III. PROPOSED METHOD

The proposed methodology employs the following: (i) Radon transform(RT) and (ii) Symbolic Factorial Discriminant Analysis (Symbolic FDA), which are described in the following sections.

A. Radon Transform

The radon transform (RT) is a fundamental tool in many areas. The 3D radon transform is defined using 1D projections of a 3D object $f(x,y,z)$ where these projections are obtained by integrating $f(x,y,z)$ on a plane, whose orientation can be described by a unit vector $\vec{\alpha}$. Geometrically, the continuous 3D radon transform maps a function \square^3 into the set of its plane integrals in \square^3 . Given a 3D function $f(\vec{x}) \square f(x, y, z)$ and a plane whose representation is given using the normal $\vec{\alpha}$ and the distance s of the plane from the origin, the 3D continuous radon transform of f for this plane is defined by

$$\begin{aligned} \mathfrak{R}f(\vec{\alpha}, s) &= \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} f(\vec{x}) \delta(\vec{x}^T \alpha - s) d\vec{x} \\ &= \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} f(x, y, z) \delta(x \sin \theta \cos \phi + y \sin \theta \sin \phi + z \cos \theta - s) dx dy dz \end{aligned}$$

where $\vec{x} = [x, y, z]^T$, $\vec{\alpha} = [\sin \theta \cos \phi, \sin \theta \sin \phi, \cos \theta]^T$, and δ is Dirac's delta function defined by

$$\delta(x) = 0, x \neq 0, \int_{-\infty}^{\infty} \delta(x) dx = 1. \text{ The radon transform maps the spatial domain } (x,y,z) \text{ to the domain } (\vec{\alpha}, s) \text{ [14,15].}$$

B. Symbolic Faces

Consider the 3D range face images $\Gamma_1, \Gamma_2, \dots, \Gamma_n$, each of size $N \times M$, from a 3D face image database. Let $\Omega = \{\Gamma_1, \Gamma_2, \dots, \Gamma_n\}$ be the collection of n face images of the database, which are first order objects. Each object $\Gamma_l \in \Omega$, $l = 1, 2, \dots, n$, is described by a feature vector $(\tilde{Y}_1, \dots, \tilde{Y}_p)$, of length $p = NM$, where each component \tilde{Y}_j , $j = 1, 2, \dots, p$, is a single valued variable representing the range values of the 3D face image Γ_l . An image set is a collection of 3D range face images of m different subjects; each subject has same number of images but with different facial expressions and illuminations. There are m number of second order objects (face classes) denoted by c_1, c_2, \dots, c_m , each consisting of different individual images $\Gamma_l \in \Omega$. We denote the set $E = \{c_1, c_2, \dots, c_m\}$ and $c_i \subseteq \Omega$, $i = 1, 2, \dots, m$. The feature vector of each face class $c_i \in E$ is described by a vector of p interval variables Y_1, Y_2, \dots, Y_p , and is of length $p = NM$. The interval variable Y_j of face class c_i is declared by $Y_j(c_i) = [x_{ij}, \bar{x}_{ij}]$, where x_{ij} and \bar{x}_{ij} are minimum and maximum intensity values, respectively, among j^{th} range values of all the images of face class c_i . This interval incorporates information of the variability of j^{th} feature inside the i^{th} face class. We denote $X(c_i) = (Y_1(c_i), \dots, (Y_p(c_i)))$. The vector $X(c_i)$ of symbolic variables is recorded for each $c_i \in E$, and can be

described by a symbolic data vector which is called as symbolic face : $X(c_i) = (a_{i1}, a_{i2}, \dots, a_{ip})$, where $a_{ij} = Y_j(c_i)$, $j = 1, 2, \dots, p$ [13,14] We represent the m symbolic faces by a $m \times p$ matrix :

$$\underline{X} = \begin{pmatrix} a_{11} & \dots & a_{1p} \\ \cdot & \cdot & \cdot \\ a_{m1} & \dots & a_{mp} \end{pmatrix} = (a_{ij})_{m \times p}$$

C. Symbolic PCA

The symbolic PCA takes as input the matrix \underline{X} containing m symbolic faces pertaining to the given set Ω of images. We use centers method, which essentially applies the conventional PCA method to the centers $x_{ij}^c \in \mathfrak{R}$ of the interval $[\underline{x}_{ij}, \bar{x}_{ij}]$, that is,

$$x_{ij}^c = \frac{x_{ij} + \bar{x}_{ij}}{2}$$

where $j = 1, \dots, p$ and $i = 1, \dots, m$. The $m \times p$ data matrix \underline{X}^c containing the centers x_{ij}^c of the intervals α_{ij} for m symbolic faces given by :

$$\underline{X}^c = \begin{pmatrix} x_{11}^c & \dots & x_{1p}^c \\ \cdot & \cdot & \cdot \\ x_{m1}^c & \dots & x_{mp}^c \end{pmatrix}$$

The mean vector ψ of \underline{X}^c is defined by $\psi = [\psi_j]$, where $\psi_j = \frac{1}{m} \sum_m x_{ij}^c$, $j = 1, 2, \dots, p$. Each row vector of \underline{X}^c differs from the mean vector ψ by the vector $\Phi_i = (x_{i1}^c, x_{i2}^c, \dots, x_{ip}^c) - \psi$. We define the matrix Φ as $\Phi = [\Phi_1, \Phi_2, \dots, \Phi_m]$. The covariance matrix C is obtained as $C = \Phi' \Phi$. Then, we calculate the eigenvalues $\lambda_1 \geq \lambda_2 \geq \dots, \lambda_m \geq 0$ and the corresponding orthonormalized eigenvectors $y_1, y_2, \dots, y_m \in \mathfrak{R}^m$ of the covariance matrix C . The eigenvectors of the symbolic PCA can be obtained as $V_m = \Phi Y_m$, where $Y_m = (y_1, \dots, y_m)$ is the $m \times m$ matrix with columns y_1, y_2, \dots, y_m and V_m is the $p \times m$ matrix with corresponding eigenvectors v_1, v_2, \dots, v_m , as its columns. The subspace is extracted from the $p \times m$ dimensional space by selecting S number of eigenvectors, which contain maximum variance and are denoted by v_1, v_2, \dots, v_s , corresponding to eigenvalues $\lambda_1 \geq \lambda_2 \geq \dots, \lambda_s$. The weights W_{ik} for i^{th} symbolic face, $i = 1, 2, \dots, m$, are computed as $W_{ik} = V_k^T (x_{ij}^c - \psi)$. where $k = 1, 2, \dots, S$. The weights of i^{th} symbolic face from the feature vector $(W_{i1}, W_{i2}, \dots, W_{is})$ of the i^{th} symbolic face [11-13]. The weights of test image I_{test} are computed by projecting the test image into face subspace as :

$$W_{testk} = v_k^T (I_{test} - \Psi).$$

D. Proposed Methodology

The Figure 1 shows the overview of proposed framework. The algorithms of the training phase and the testing phase of the proposed method are given below:

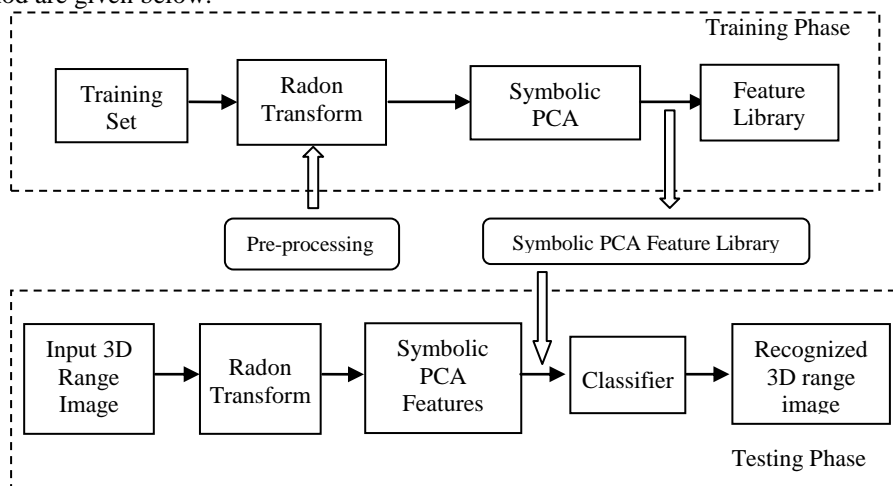


Figure 1. Overview of proposed framework

Algorithm 1: Training Phase

1. Input the range image I_1 from the training set containing M images.
2. Apply Radon transform, from 0° to 180° orientations (in steps of h), to the input range image I_1 yielding a binary image I_2 .
3. Superpose the binary image I_2 obtained in the Step 2 on the input range image I_1 to obtain the cropped facial range image I_3 .
4. Repeat the Steps 1 to 3 for all the M facial range images in the training set.
5. Apply Symbolic PCA to the set of cropped facial range images obtained in the Step 4 and obtain M Eigen faces.
6. Compute the weights w_1, w_2, \dots, w_p for each training face image, where $p < M$ is the dimension of Eigen subspace on which the training face image is projected.
7. Store the weights w_1, w_2, \dots, w_p for each training image as its facial features in the Symbolic PCA feature library of the face database.

Algorithm 2: Testing Phase

1. Input the test range image Z_1 .
2. Apply Radon transform, from 0° to 180° orientations (in steps of h), to the input range image Z_1 yielding a binary image Z_2 .
3. Superimpose the binary image Z_2 on Z_1 to obtain the cropped facial image Z_3 .
4. Compute the Symbolic weights $w_i^{test}, i = 1, 2, \dots, p$, for the test image Z_1 by projecting the test image on the Symbolic PCA feature subspace of dimension p .
5. Compute the Euclidian distance D between the feature vector w_i^{test} and the feature vectors stored in the Symbolic PCA feature library.
6. The face image in the face database, corresponding to the minimum distance D computed in the Step 5, is the recognized face.
7. Output the texture face image corresponding to the recognized facial range image of the Step 6.

IV. EXPERIMENTAL RESULTS AND DISCUSSION

The proposed method is implemented using Intel Core 2 Quad processor @ 2.66 GHz machine and MATLAB 7.9. In the training phase, 10 frontal face images with different expression of each 50 subjects are selected as training data set. In the testing phase, randomly chosen 200 face images of the Texas 3D face database with variations in facial expressions are used. The sample training images which are used for our experimentation are shown in the Figure 2, and their corresponding texture images are shown in the Figure 3.

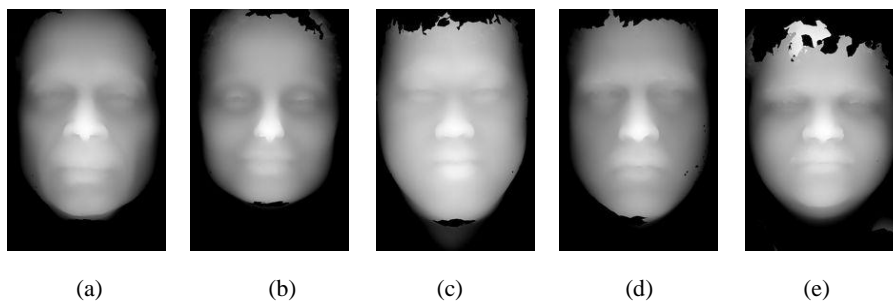


Figure 2. Sample range images of the training set.

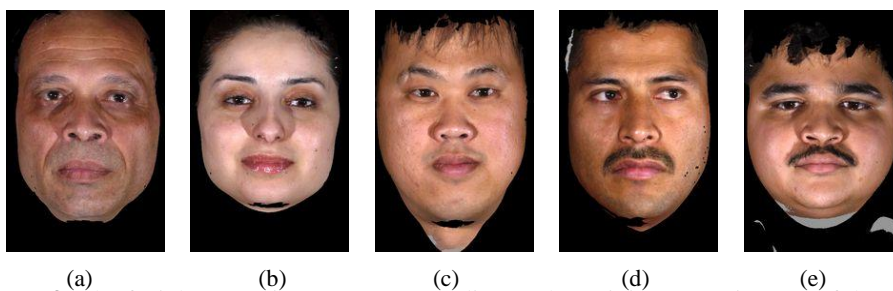


Figure 3. The facial texture images corresponding to the training range images of the Figure 2

The recognition rates obtained by the proposed (RT+ Symbolic PCA) approach is compared with PCA (alone), Symbolic PCA and RT+PCA methods [15] is presented in the Table 1. The graph of recognition rates versus the number

of eigenfaces is shown in the Fig.4 for the proposed method (RT + Symbolic PCA) with other PCA, Symbolic PCA and RT + PCA methods. It is observed that the recognition rate improves as the number of eigen faces is increased. It is 98% for 40 eigenfaces in case of proposed method using SVM classifier. Further, the proposed method based on RT and Symbolic PCA outperforms the PCA method.

Table 1. The face recognition accuracy(%) and recognition times (in Secs.) obtained by the proposed method using different number of eigen faces and LDA components.

No.of Eigen faces	PCA [18]		RT+PCA [21]		RT + Symbolic PCA (Proposed Method)			Average Time taken (in secs.)
	Accu racy %	Time (in secs.)	Accu racy %	Time (in secs.)	Recognition Accuracy (in %)			
					Minimum Distance Classifier	KNN (K=5)	SVM	
5	58.5	9.813	60.1	9.941	61.00	61.50	62.00	9.130
10	76.1	9.822	77.5	9.950	77.60	78.00	79.00	9.157
15	81.5	9.824	84.36	9.950	85.00	85.30	85.50	9.270
20	87.1	9.828	90.19	9.953	91.00	91.50	91.50	9.286
25	87.61	9.834	94.1	9.953	94.10	94.50	94.70	9.592
30	88.5	9.845	94.16	9.953	95.00	96.00	96.50	10.031
35	89.11	9.861	95.2	10.170	96.00	96.00	96.80	10.081
40	89.47	10.161	95.3	10.172	97.00	97.00	98.00	10.970

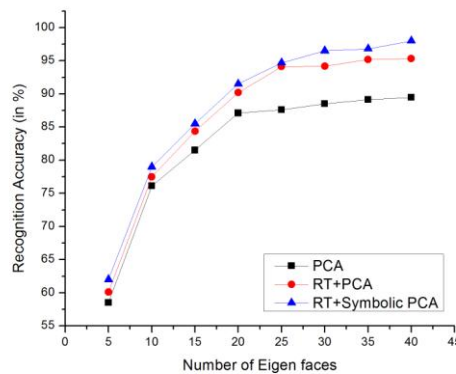


Figure 4. The comparison of the recognition accuracy (%) versus the number of eigenfaces for the proposed method (RT + Symbolic PCA) with the methods in [21]

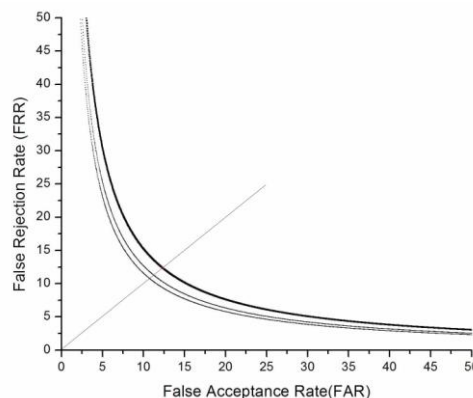


Figure 5. Receiver operating characteristic (ROC) curves for the proposed method for Bosphorus, Texas and CASIA 3D face databases with equal error rates 15.5642, 14.1897 and 11.5310, respectively

V. CONCLUSION

In this paper, we have proposed a novel hybrid method for Three Dimensional (3D) face recognition using Radon transform with Symbolic PCA based features on 3D range face images. In this method, the Symbolic PCA based feature computation takes into account face image variations to a larger extent and has advantage of dimensionality reduction. The experimental results yield 97% recognition performance with low complexity and a small number of features, which compares well with other state-of-the-art methods. The experimental results demonstrate the efficacy and the robustness of the method to illumination and pose variations. The recognition accuracy can be further improved by considering a larger training set and a better classifier.

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