



## Survey of Side Channel Attacks on ECC

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**Abstract:** Side-channel analysis is a powerful technique discovered by P. Kocher. The principle consists in monitoring some side-channel information like the running time, the power consumption, or the electromagnetic radiation. From the monitored data, the attacker tries to deduce the inner-workings of the algorithm and thereby to retrieve some secret information. This survey is aimed to analyse the performance of elliptic curve cryptosystem under side channel attacks. The main advantage of Elliptic curve cryptography is smaller key size, it is mostly used for public key infrastructure, but the side channel analysis is now well understood by the implementer.

**Keywords:** Elliptic Curve Cryptography, Side Channel Attack, Running Time, Power Consumption, Electromagnetic Radiation.

### I. INTRODUCTION

Provable security becomes more and more popular in the cryptographic community. It is now common to see it as an attribute of a cryptosystem. Provable security is at the protocol level, a harder task may be to evaluate the security of a cryptosystem at the implementation level. Rather than considering a cryptosystem as a black-box, we may assume that some sensitive data can leak during the course of the execution of a (naively implemented) crypto-algorithm. Side-channel analysis is a powerful technique re-discovered by P. Kocher in 1996. The principle consists in monitoring some side-channel information like the running time, the power consumption, or the electromagnetic radiation. Next, from the monitored data, the attacker tries to deduce the inner-workings of the algorithm and thereby to retrieve some secret information. When there is a single measurement, the process is referred to as a *simple* side channel analysis; and when there are several measurements handled together with statistical tools, the process is referred to as *differential* side-channel analysis.

### II. ELLIPTIC CURVE CRYPTOGRAPHY

Elliptic Curve Cryptography (ECC) is a public key cryptography. In public key cryptography each user or the device taking part in the communication generally have a pair of keys, a public key and a private key, and a set of operations associated with the keys to do the cryptographic operations. Only the particular user knows the private key whereas the public key is distributed to all users taking part in the communication. Some public key algorithm may require a set

of predefined constants to be known by all the devices taking part in the communication. 'Domain parameters' in ECC is an example of such constants. Public key cryptography, unlike private key cryptography, does not require any shared secret between the communicating parties but it is much slower than the private key cryptography.

The mathematical operations of ECC is defined over the elliptic curve  $y^2 = x^3 + ax + b$ , where  $4a^3 + 27b^2 \neq 0$ . Each value of the 'a' and 'b' gives a different elliptic curve. All points (x, y) which satisfies the above equation plus a point at infinity lies on the elliptic curve. The public key is a point in the curve and the private key is a random number. The public key is obtained by multiplying the private key with the generator point G in the curve. The generator point G, the curve parameters 'a' and 'b', together with few more constants constitutes the domain parameter of ECC. One main advantage of ECC is its small key size. A 160-bit key in ECC is considered to be as secured as 1024-bit key in RSA.

The principal attraction of ECC compared to RSA is that it offers equal security for a far smaller key size, thereby reducing processing overhead. The addition operation in ECC is the counterpart of modular multiplication in RSA, and multiple additions are the counterpart of modular exponentiation. To form a cryptographic system using elliptic curves, we need to find a "hard problem". All systems rely on the difficulty of a mathematical problem for their security. To explain the concept of difficult mathematical problem, the notion of an algorithm is required. To analyze how long an algorithm takes, computer scientists introduced the idea of polynomial time algorithms and exponential time algorithms. An algorithm runs quickly if it is polynomial time algorithm, and slowly if it is exponential time algorithm. Therefore, easy

problems equate with polynomial time algorithms, and difficult problems equate with exponential time algorithms. When looking for a mathematical problem on which to base a public key cryptographic system, cryptographers search for a problem for which the fastest algorithm takes exponential time. The longer it takes to compute the best algorithm for a problem, the more secure a public key cryptosystem based on that problem will be. Three types of systems are considered secure and efficient: the Integer Factorization Systems (RSA), the Discrete Logarithm Systems (DSA), and the Elliptic Curve System (Elliptic Curve Discrete Logarithm System). In RSA, given an integer  $n$  which is the product of two large primes  $p$  and  $q$  such that,

$$n = pq. \quad (1)$$

It is easy to calculate  $n$  given  $p$  and  $q$  but it is difficult to determine  $p$  and  $q$  given  $n$  for large values of  $n$ . The U.S. government's Digital Signature Algorithm (DSA) is based on discrete logarithm problem modulo a prime  $p$ . Given an integer  $g$  between 0 and  $p-1$ , and  $y$  which is the result of exponentiation of  $g$ , we have

$$y = g^x \pmod{p} \text{ for some } x. \quad (2)$$

The discrete logarithm problem modulo  $p$  is to determine the integer  $x$  for a given pair  $g$  and  $y$ . The Elliptic Curve Cryptosystem (ECC), whose security rests on the discrete logarithm problem over the points on the elliptic curve. The main attraction of ECC over RSA and DSA is that the best known algorithm for solving the underlying hard mathematical problem in ECC (the elliptic curve discrete logarithm problem (ECDLP) takes full exponential time. RSA and DSA take sub-exponential time. This means that significantly smaller parameters can be used in ECC than in other systems such as RSA and DSA, but with equivalent levels of security. A typical example of the size in bits of the keys used in different public key systems, with a comparable level of security (against known attacks), is that a 160-bit ECC key is equivalent to RSA and DSA with a modulus of 1024 bits. The lack of a sub-exponential attack on ECC offers potential reductions in processing power and memory size. These advantages are especially important in applications on constrained devices. In practical terms, the performance of ECC depends mainly on the efficiency of finite field computations and fast algorithms for elliptic scalar multiplications. In addition to the numerous known algorithms for these computations, the performance of ECC can be increased by selecting particular underlying finite fields and/or elliptic curves. For ECC, we are concerned with a restricted form of elliptic curve that is defined over a finite field. Of particular interest for cryptography is what is referred to as the elliptic group mod  $p$ , where  $p$  is a prime number. This is defined as follows. Choose two nonnegative integers,  $a$  and  $b$ , less than  $p$  that satisfy:

$$4a^3 + 27b^2 \pmod{p} \neq 0. \quad (3)$$

Then  $E_p(a, b)$  denotes the elliptic group mod  $p$  whose elements  $(x, y)$  are pairs of nonnegative integers less than  $p$ , satisfying:

$$y^2 = x^3 + ax + b \pmod{p} \quad (4)$$

Together with the point at infinity  $O$ . The elliptic curve discrete logarithm problem can be stated as follows. Fix a prime  $p$  and an elliptic curve.

$$Q = xP \quad (5)$$

Where  $xP$  represents the point  $P$  on elliptic curve added to itself  $x$  times. Then the elliptic curve discrete logarithm problem is to determine  $x$  given  $P$  and  $Q$ . It is relatively easy to calculate  $Q$  given  $x$  and  $P$ , but it is very hard to determine  $x$  given  $Q$  and  $P$ .

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### III. SIDE CHANNEL ATTACKS ON ECC

Side-channel analysis is a powerful technique re-discovered by P. Kocher in 1996. The principle consists in monitoring some side-channel information like the running time, the power consumption, or the electromagnetic radiation. Next, from the monitored data, the attacker tries to deduce the inner-workings of the algorithm and thereby to retrieve some secret information. When there is a single measurement, the process is referred to as a *simple* side channel analysis; and when there are several measurements handled together with statistical tools, the process is referred to as *differential* side-channel analysis [1] [3].

Side channel attacks based on following Parameters

- Time Analysis
- Power Analysis
- Electromagnetic analysis

On the basis of these parameters, there are two types of attacks on ECC

➤ **Simple Side Channel Analysis**

When there is a single parameter measurement.

➤ **Differential Side Channel Analysis**

When there are several parameter measurements handled together with statistical tools.

### IV. ATTACKS ON IMPLEMENTATIONS

Several classes of attacks can be distinguished. The most straightforward attack is a physical attack directly to the silicon. This is a powerful method if a probing point is available. For instance, it is easy to retrieve secret information by probing the data on a bus. The fault induction attack is a well-known technique that works by disturbing the device to induce errors in the computation. These attacks are named *active attacks* after the technique. A possibly more dangerous type of attack, undetectable for the embedded system, is called *passive attacks*. These attacks are based on measuring physical characteristics leaking from side-channels of the embedded system. Timing Analysis (TA) checks the computation time. If the execution time varies with the data or the key used in the computations, this can be detected by the

attacker. Simple Power Analysis (SPA) measures the power consumption during cryptographic operations and guesses the actual types of computations. In, Kocher *et al.* introduced Differential Power Analysis (DPA) that also considers effects correlated to data values. Electromagnetic Analysis (EMA) and Acoustic Analysis (AA) were also introduced as effective SCA examples

## V. THE ATTACKER'S TASK

The attacker has the ability to observe a sequence of elliptic curve operations, thus, the attacker's aim is to calculate and exploit the probabilities of certain sequences of bits given an observed sequence of elliptic curve operations. Using the information of such conditional probabilities, the key-space that has to be searched to find the correct ephemeral key, can be significantly reduced. This is because certain combinations of patterns in the power trace and certain combination of digits are less likely than the others (or even not possible at all). The attacker's task can be stated in a more formal way. Let  $X$  be a random variable that denotes a sequence of elliptic-curve operations and  $|X|$  the length of  $X$  (i.e. the number of elliptic-curve operations in this sequence). For example,  $X = \text{"DDD"}$  (i.e. the realization of the random variable  $X$  consists of three consecutive elliptic-curve point-double operations) thus  $|X| = 3$ , or  $X = \text{"DAD"}$  (i.e. the realization of the random variable  $X$  consists of an elliptic-curve point-double operation, an elliptic-curve point-addition operation and an elliptic-curve point-double operation) thus  $|X| = 3$ . Let  $Y$  be a random variable that denotes a sequence of digits in the digit representation of  $k$  and  $|Y|$  the length of  $Y$  (i.e. the number of digits). For example  $Y = \text{"000"}$  (i.e. the realization of the random variable  $Y$  consists of three consecutive zeros) thus  $|Y| = 3$ , or  $Y = \text{"01"}$  (i.e. the realization of the random variable  $Y$  consists of a zero and a one digit) thus  $|Y| = 2$ . Then the attacker's goal is to calculate and exploit the conditional probability

For many different realizations  $x$  of  $X$  and  $y$  and  $Y$ . Equation 1 is the mathematical definition for the conditional probability. Enhancing Simple Power-Analysis Attacks on Elliptic Curve Cryptosystems, It is an important observation that the calculation of the right hand side of (1) requires the knowledge of the probability to be in a specific state of the point multiplication algorithm (the terminology used here will be explained in the next section). This is because in order to calculate the probabilities  $P(X = x)$ , one has to calculate the sum of the probabilities of all possible sequences of digits that lead to the pattern  $x$ . Since such a sequence can basically start from any state of the algorithm, the probabilities are dependent on the probability of the starting-state.

The basic principles of how to apply power analysis attacks on elliptic curve cryptosystems have been discussed. To counteract both simple power analysis attacks and (first order) differential power-analysis attacks there are basically two things that have to be done. Firstly, one has to randomize the expressions (i.e. the coordinates) of calculated

points. This can be done by using randomized projective coordinates (DPA countermeasure). Secondly, one has to conceal the ephemeral key. It would be optimal if there would be no statistical relationship between the sequence of elliptic-curve operations and the bits of the ephemeral key (SPA countermeasure). Countermeasures applicable to arbitrary curves fixing the sequence of elliptic-curve operations have been presented by Coron, Moller and Izu. Countermeasures applicable to arbitrary curves not fixing the sequence of elliptic-curve operations have been presented by Oswald and Brier. Countermeasures applicable to special curves fixing the sequence of elliptic-curve operations have been presented by Hasan and by Okeya. Countermeasures applicable to special curves not fixing the sequence of elliptic-curve operations have been presented by Liardet and Joye.

## VI. VARIOUS PARAMETRIC ATTACKS ON ECC

### Time Analysis Attack

Kocher presented the timing-attacks: Attackers carefully measure the amount of time required to perform the private key operations, so that they might be able to decide fixed Diffie-Hellman exponents [11]. This attack could be applicable to the elliptic curve cryptosystems including ECDSA. Time required to perform the conventional scalar multiplication algorithm based on the Weierstrass-form depends on the bit-patterns (and on the ratio between the number of zeros and the number of ones) of the secret value [3]. Where as we show that the scalar multiplication on the Montgomery-form elliptic curve does *not* depend on the bit-patterns (nor on the ratio between the number of zeros and the number of ones) of the secret value. It has exactly seven multiplications and four square-multiplications on  $\mathbb{F}_p$  per bit. This is due to the specific algorithm for computing scalar multiplication  $nP$  from  $P$ , which repeatedly calculates either  $(2mP, (2m + 1)P)$  or  $((2m + 1)P, (2m + 2)P)$  from  $(mP, (m + 1)P)$  in the Montgomery-form elliptic curves. The computation via by choosing a representative in the projective coordinates randomly is also useful for making it more difficult to measure the amount of time required. We compute the scalar  $d$  multiplications on the affine coordinates  $(x, y)$  via a corresponding projective coordinates  $(kx, ky, k)$ , where  $k$  is randomly chosen. Thus, Montgomery-form elliptic curves are shown to be useful for public-key cryptosystems from the point of view of not only efficient implementation but also protection against timing-attacks.

### Power Analysis Attack

Power attacks arise from the actual implementation of the cryptosystems, which differ from the ideal cryptosystems. There are leakages of information in addition to input and output data while the cryptographic devices (e.g. smart card) execute cryptographic transactions (e.g. signature, encryption, decryption) [11]. An attacker may use the leakages for his estimate. In 1996, Kocher proposed timing attack. Timing attack is one of the power attacks in which an attacker uses

timing of execution for his estimate of the secret key. Recently, Kocher et al. proposed DPA (Differential Power Analysis) and SPA (Simple Power Analysis) DPA is a power attack in which an attacker uses power consumption and analyzes such data statistically, and SPA is an attack without statistical analysis[7]. Coron generalized DPA to elliptic curve cryptosystems with the following SPA-immune scalar multiplication algorithm. for the purpose of constructing cryptosystems with immunity to DPA, we explain characteristics of DPA how an attacker estimates the secret key in the attack. The point of this attack is “a difference between executing procedures (non-symmetry)” and “an appearance of a predicted special value”. First, the executing procedure of typical cryptographic transaction depends on the secret key. Consequently, the executing procedure of cryptographic transaction differs from secret key to secret key. If an attacker finds the difference of the executing procedure from leakages, he is able to derive the information on the secret key. Actually, since it is hard to find the difference of executing procedure as it is, he treats it statistically and makes its bias big, and finally he finds the difference of the executing procedure. Next, if an appearance of some specific value on the cryptographic transaction depends on the secret key, an attacker is able to detect the secret key by whether the value appears on the execution or not.

#### Electromagnetic Analysis Attack

Nowadays, CMOS is by far the most commonly used technology to implement digital integrated circuits. A CMOS gate consists of a pull-up network with p-MOS transistors and a pull-down network with n-MOS transistors. Those networks are complementary: when the input is stable, only one of the two networks conducts. The most simple logic gate is an inverter; its power consumption is representative for all logic ports and gives a general image of the power consumption in a CMOS circuit. During the functioning of the inverter, 3 types of power consumption can be distinguished. The leakage current, the current that flows from the power source to the ground during the switching from 0 to 1 (short-circuit current) and the current used to charge and discharge the different capacitors in a digital network (dynamic power consumption). The last one causes the biggest power consumption in present designs. Important to note is that these capacitors are necessary to maintain the two different logic levels. In addition, all capacitors for each gate differ, which results in a different power consumption of the different gates according to the data being processed [23]. The sudden current pulse that occurs during the transition of the output of a CMOS gate causes a variation of the electromagnetic field surrounding the chip; this can be monitored for example by inductive probes which are particularly sensitive to the related impulsion.

Two types of electromagnetic analysis attacks are distinguished. In a *simple electromagnetic analysis* (SEMA) attack, an attacker uses the information from one electromagnetic radiation measurement directly to determine (parts of) the secret key [11]. In a *differential electromagnetic*

*analysis* (DEMA) attack, many measurements are used in order to filter out noise and the key is derived using a statistical analysis. While SEMA exploits the relationship between the executed operations and the electromagnetic radiation, DEMA exploits the relationship between the processed data and the electromagnetic radiation [23]. A SEMA attack is typically used when there is a conditional branch in the algorithm, which results in a different radiation pattern whenever the branch is taken. A DEMA attack uses the property that processing different data needs a distinct amount of power and radiates a different field.

#### VII DESIGN FLOW OF TIME ANALYSIS ATTACK

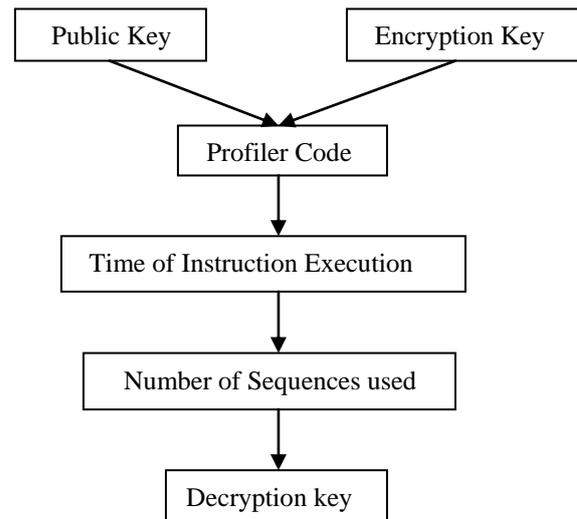


Figure1: Design flow of Time Analysis Attack

Scalar point-multiplication consists of a sequence of point-addition, point-subtraction and point-doubling operations. The attacker's goal is to learn the key using the information obtained from carefully observing the running Time required for a complete scalar point-multiplication. Every elementary field-operation has its unique running time required. The sequence of elementary field-operations that form the point-addition operation has a different running Time required than the sequence of elementary field operations that form the point-doubling operation. Profiler code analyses the time required to execute the set of instructions written under it.

#### VIII CONCLUSION

We have studied different parametric Attacks, like time analysis Attack, Power Analysis Attack, Electromagnetic Analysis Attack. The different parameters used are Time consumption, power consumption, and electromagnetic radiations to produce result. Finally describes the design flow of timing attack on Elliptic curve cryptography in public key Infrastructure scheme.

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